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# Temperature fluctuations underneath the ice in Diamond Lake, Hennepin County, Minnesota

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[1] Diamond Lake in Minnesota is covered every winter with ice and snow providing a modified thermal insulation between water and air. Autonomous temperature sensors, data loggers, were placed in this lake so that hourly measurements could be obtained from the snow-covered ice and water. The sensors that became frozen measured damped and delayed thermal response from the air-temperature fluctuation. Those sensors that were deeper within the snow-covered ice measured continuous, almost constant, temperature values near freezing. Several of them were within the liquid water and responded with a fluctuation of 24 h periods of amplitudes up to  $0.2^{\circ}$ C. Our analysis of the vertical temperature profiles suggested that the source of periodic water heating comes from the lake bottom. Because of the absence of daily temperature variations of the snow-covered ice, the influence of the airtemperature fluctuation can be ruled out. We attribute the heating process to the periodic inflow of groundwater to the lake and the cooling to the heat diffusion to the overlying ice cover. The periodic groundwater inflow is interpreted due to solid Earth tides, which cause periodic fluctuations of the groundwater pressure head.

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#### Introduction 1.

[2] The formation of the ice over lakes and its thickening is a result of air temperature, wind condition, and snow cover [Adams and Roulet, 1980; Adams and Prowse, 1981; Bengtsson, 1986; Gow and Langston, 1977; Jones, 1969; Kirillin et al., 2012]. Because the thermal conductivity of the ice is 1–2 orders of magnitude larger than that of the snow, any thickness of snow over ice provides a significant thermal barrier between temperature of the air and the temperature of the ice. Therefore, the formation of the ice over the lake depends on how much snow covers the lake. Another type of ice is a snow ice formation that is initiated when the mass of snow on the ice causes the ice to sink below the pond's water level, and water flows up through fractures to the ice surface. The thermal resistance of snow becomes a factor when freezing the slush into the snow ice. The phase change regime of ice and its response to air-temperature variability, snow accumulation, and ice formation have been shown to consistently decrease toward the bottom of the ice/water interface [Gould and Jeffries, 2005].

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Such fluctuation stays within a fraction of the degree, and 96 the ice creates a natural protection from the environmental 97 fluctuation [Kirillin et al., 2009, 2012; Malm et al., 1997a; 98 Zdorovennova, 2009].

[3] The thermal structures in the vicinity of the ice-water 100 and water-sediment interfaces have been given attention in 101 order to characterize the amount of heat released from sedi-102 ments [Zdorovennova, 2009]. When there are no other heat sources (heat exchange with the atmosphere, solar radiation penetrating through the ice, river inflow), the heat flux from 105 the bottom relates to heat accumulation from the previous 106 summer. Because the littoral zone is shallower there is more of the heat captured near the shore than there is in the deeper parts of the lake. Such heat excess from bottom 109 sediments near the shore was reported from small shallow 110 Karelian Lakes [Malm et al., 1997a, 1997b]. However, 111 multiple water temperature measurements near bottom 112 sediments in the Lake Vendyurskoe revealed enigmatic 113 temperature structures with 1 day period that could not be 114 explained by baroclinic seiche under the ice [Zdoroven-115 nova, 2009] with a possibility that such variation may 116 relate to the Poincare type waves [Kirillin et al., 2009]. Kir-117 illin also measured details of the temperature variation of 118 ice-covered Lake Müggelsee in Germany and saw the peri-119 ods of 24, 11, and 8 h in their record. These fluctuations 120 were independent from the amount of snowfall or its melt-121 ing and indicated that water temperature fluctuations are 122 separated from its solar heating [Kirillin et al., 2009]. 123

[4] Observation of the 1 day temperature fluctuation 124 periods in shallow lakes suggests a presence of fundamen-125 tal forces controlling the winter lake environment. Ice over 126 lakes forms natural protection from environmental 127 extremes important for survival of life forms and may be 128

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critical for development of life, both on Earth and on other bodies of the solar system where the interface between the liquid water and ice is critical for the origin of life. Similar conditions exist not only at the bottoms of numerous lakes whose surface water freezes but also at water/ice interfaces on the top of completely enclosed glacial lakes like the Lake Vostok in Antarctica, similar lakes that are believed to be buried on Mars, as well as the interface of the ice and water on Europa, the moon of Jupiter [Kletetschka et al., 2006]. The projected broad relations warrants furthering our understanding of the forces responsible for this not completely understood phenomena. Even though the work by Kirillin and Zdorrovenova was done in fairly shallow lakes, it shows that the fluctuating temperature signal is confined to the sediment/water boundary and disappears toward the ice/water boundary. We chose even shallower lake, the Diamond Lake, Minnesota, with average depth of 2 m.

#### **Temperature Monitoring** 2.

[5] Autonomous data loggers, iButtons, were utilized to measure not only the speed of the ice growth in the Diamond Lake near Dayton and Rogers, Minnesota (geographical coordinates: longitude -93.506°, latitude 45.201°), but also the environmental conditions that are being kept at the very bottom of the lake ice thickening. The Diamond Lake is small (1.64 km<sup>2</sup>) and shallow (maximum depth = 2.44 m, mean depth = 1.98 m). It is 1.4 km long in NS and 1.6 km wide in EW directions, with its 7.24 km

shoreline, and stores about 3 km<sup>3</sup> of water (see Figure 1). F195 The bottom of this lake consists of coarse silt sediment. The water is being fed into this lake from the marshes in SW near Rogers town. Water exits in SE via the Diamond Creek flowing into Hyden Lake and further toward the Mis-sissippi River via the Elm Creek. Experimental site was designed near the north shore where the depth of the Dia-mond Lake was 58 cm. The ice that formed over the lake was periodically covered with snow; whose depth was recorded at KMSP weather station, 40 km southeast from AQ2204 the sensor location (http://mesowest.utah.edu/index.html). 

[6] The iButton data loggers (model DS1922L-F50), with a temperature resolution of 0.06°C were used as the autonomous sensors. They contained computer chips enclosed in 16 mm diameter  $\times$  6 mm height stainless cylindrical cases. Such package is resistant to environmental hazards such as dirt, moisture, and shock. These devices were made by Embedded Data Systems, LLC (http:// www.maxim-ic.com).

[7] Ten sensors were placed in the lake water just after it frozen over on 25 November 2010, when the ice was only 2 cm thick. They were retrieved on 29 March 2011. Sensors were programmed to include the period of interest from 3 December till 19 February. Devices were submerged at 2, 5, 8.5, 12, 17, 22, 24, 26, 28.5, and 30.5 cm below the water level taped to a 1 m of plastic rope, suspended down from the floating container (Figure 1), and anchored with the metal hook at the 58 cm deep bottom. They were programmed to register temperature every 60 min with a resolution of 0.06°C. After data retrieval we checked all



Figure 1. Ten temperature data loggers were placed at the northern shore of the Diamond Lake in Dayton, Minnesota. In the bathymetric map black arrows show the lake water input and output. The gray arrow shows location of the sensors. The upper inset is schematic diagram showing the placement of the sensors. The depth of the lake at the location of the sensors is 58 cm. The shore was 110 cm away. The ice has reached the thickness of 20 cm and stayed constant during most of the measurement period.

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**Figure 2.** (top) Overall record of temperatures from the eight sensors below the surface, air temperature, barometric pressure, and snow cover (dashed) from Diamond Lake, Minnesota, over the period of 78 days in winter 2010/2011. In the upper section the ice (lower set of four curves) and water (upper set of three curves), temperature was measured by 10 sensors distributed in depths from 2 to 30.5 cm. Curves for data loggers at 5.5 and 28.5 cm are not shown for clarity. The air-temperature curve, snow cover, and barometric pressure records were obtained from the station KMST, 40 km southeast apart.

sensors, and they all worked properly and were suitable for other missions.

### 3. Data and Results

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[8] Temperature records obtained during the period between the two thaws at the beginning of December and F2 the end of February are displayed in Figure 2. This period was characterized by a continuous snow cover and mostly freezing air temperatures. The temperature data separate our devices into two groups (Figure 2): the measurements in ice (sensors at the depths of 2.0, 5.0, 8.5, 12.0, and 17.0 cm; lower group of four curves in the upper region) and measurements in water (sensors at the depths of 22.0, 24.0, 26.0, 28.5, and 30.5 cm; upper group of curves). During the above-mentioned period the temperature in ice at the depth of 2 cm varied between  $-0.06^{\circ}$ C and  $-1.54^{\circ}$ C with minimum after small thaw at the end of December, when the snow cover decreased from 40 down to 20 cm. Temperature at this depth (at the margin of ice) shows strong attenuation of variation of surface air temperature (SAT). This phenomenon is more visible during the month of December due to lower thermal conductivity of powder snow. Several tens of centimeters of powder snow was providing a good thermal insulation for most of the measurement period. The ice temperature at the depth of 17 cm has been monotonous and insensitive to the short- and/or longterm SAT variations. The ice thickness remained between 17 and 22 cm (see constant positive temperature of the sensor at 22 cm and zero-subzero temperatures of the sensor at 17 cm in Figure 2) with the phase boundary moving slightly down during the second half of the observational period (see small decrease of temperature at the depth of 17 cm in Figure 2).

[9] Similar to the temperature in ice, the water temperature (upper group of curves in Figure 2) increased with the depth in general. There are visible short- (days) and long-term (several days) temperature variations in all depths dur-ing the course of measurement. Long-term variations are 351 stronger at the deepest level of 30.5 cm near the bottom and are attenuated upward. Short-term variations are atte-nuated upward too, but only during the first period of the measurement until about 10 January. In the second period the amplitude of variations near the ice increased, whereas the amplitude at the depth of 30.5 cm stayed similar to the first period.

[10] Temperature gradient throughout the observational period was positive (see Figure 3), and the maximum tem-**F**30 perature at the depth of 30.5 cm was lower than 1°C. This means that the heat is coming from the lake bottom, and free convection can be ruled out due to the highest water density near the bottom. Such situation suggests conductive heat transfer in the observed temperature profile. We used a 1-D solution of the conductive heat equation in a semi-infi-nite homogeneous medium [Carslaw and Jaeger, 1959]: 

$$\frac{\partial T}{\partial t} = k \frac{\partial^2 T}{\partial Z^2} \tag{1} \quad \begin{array}{c} 369\\ 370\\ 371 \end{array}$$

with the periodic boundary condition

$$T(z=0,t) = A \cos \omega t, \qquad (2) \quad 374$$

where *t* is the time, *z* is the depth, *T* is the temperature, *k* is 376 the thermal diffusivity,  $\omega$  is the angular velocity, and *A* represents the amplitude of the boundary temperature wave. 378 The temperature at depth *z* and time *t* can be calculated as 379

$$T(z,t) = \operatorname{Ae}^{-\alpha z} \cos(-\alpha z + \omega t), \qquad (3) \quad 38$$

where  $\alpha = \sqrt{\omega/2k}$ . It follows that the boundary condition 383 is attenuated exponentially away from the heat source, and 384





**Figure 3.** Two sets of average temperature versus lake depth profiles are shown along the thermometer array for 10–30 December 2010 (solid circles) and 15 January to 10 February 2011 (empty squares). Vertical dashed line separates data obtained from lake ice and the data obtained from lake water.

the rate of attenuation depends on the frequency (period). Note that the phase shift increases linearly with the distance from the heat source.

F4 [11] Figure 4 compares the observed and modeled thermal attenuation of amplitude and phase shift during the period from 10 to 30 December (crosses) and period from 15 January to 10 February (triangles). The mean amplitudes and phase shifts were computed over these two periods by solving for the regression constants  $a_1$ ,  $a_2$ ,  $a_3$ , and  $a_4$  that are part of the trigonometric polynomial  $T(t) = a_1 + a_1$  $a_2(\omega t) + a_3 \sin(\omega t) + a_4 \cos(\omega t)$ . Solid lines in Figure 4 represent computed amplitude attenuation and phase shift of the observed temperature signal based on equation (3). The source of the periodic temperature change is placed to the depth with the highest amplitude of periodic changes: 30.5 cm in December and 22.5 cm (below the ice) in January/ February. The striking fit of the observations and model in December confirms that conductive heat transfer was dominant in the observed temperature profile during that period. However, in January/February the observed and modeled curves of amplitude decay strongly diverge. We suspect that the temperature field during the second observation period is strongly affected by another variable affecting the periodic temperature changes at the water-ice contact. Perhaps, once the lake and tributaries froze over, the water below the ice drained out and left the ice somewhat suspended between the ice and water. This will be a subject of further research.

[12] Similar discrepancy emerged while monitoring the
mean temperatures of the investigated depth profile (Figure
3; from 10 to 30 December (squares) and from 15 January
to 10 February (circles)). Temperature gradient in water
(right side of graph) and ice (left side of graph) was 3.3°C/m
and 1.3°C/m over the first period and 2.1°C/m and 2.4°C/m



**Figure 4.** Observed and modeled attenuation of (top) amplitude and (bottom) phase shift of the daily temperature oscillations during the period from 10 to 30 December (crosses) and period from 15 January to 10 February (triangles). Solid lines represent computed amplitude attenuation and phase shift of observed temperature signal based on equation (3).

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502 over the second period, respectively. The corresponding heat 503 flux is lower in water than in ice with 2.0 and 2.9  $W/m^2$  dur-504 ing the first period, but 1.3 and 5.3  $W/m^2$  during the second 505 one, respectively. Calculation assumed only a conductive 506 heat transfer. The values of the temperature gradient (heat 507 flux) in water are in good agreement with other lakes in Min-508 nesota and Wisconsin [Fang and Stefan, 1996]. The discrep-509 ancy between the heat flux in water and ice during January 510 and February can be connected with the phase changes in the 511 water-ice transition zone. The heat transfer during this period 512

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cannot be explained by simple conduction theory and is beyond the scope of this paper.

[13] We summarize the outcomes of Figures 2-4 as follows:

[13] (1) The influence of daily air-temperature fluctuations on the water temperature variations can be ruled out for two reasons. First, the air-temperature variations show prevailing long periods caused by ambient weather changes, and the corresponding daily period is minor. Second, the air-temperature variation is separated from the first sensor in ice by a 20 to 40 cm thick layer of snow. At the ice depth of 2 cm, the amplitudes of air-temperature variation completely disappear. Only the long-term air-temperature variations are visible in the uppermost sensors, because the longer periods are less attenuated.

[13] (2) There is a positive temperature gradient during the whole snow-covered period (Figure 3). It suggests that the source of the heat and cold (heat sink) should be below and above of the device array, respectively. The daily temperature maxima occur at about midnight, and this disqualifies the possible origin of the water temperature variations as a response to the Sun radiation.

[13] (3) Periodic temperature variations in the water at the depth of 30.5 cm are visible during the whole observation period between the thaws. The variations are attenuated upward during the month of December, and the conductive heat transfer plays substantial role. During the month of January and the first half of February the variations in the upper part of the sensor chain under the ice cover became stronger due to other mechanisms of unknown origin.

[14] During the snow-covered period, air-temperature variations do not affect the dynamics of water temperature field. During the thaw when the snow disappears, the solar heating becomes more effective, and the radiation-driven convection starts to develop. As a result, the temperature gradient in the close vicinity of the ice-water interface is nearly permanent for most of the winter, and the heat flux from water to ice varies slightly in time [see Malm et al., 1997a, 1997b]. This is in agreement with our measurements and clearly visible in Figure 3 where the mean temperature gradient between two detectors just under the ice cover is similar during both of the above-mentioned periods (December and January/February). Warming from the bottom is driven by the heat stored in the bottom sediments during the summer [Fang and Stefan, 1996]. This process starts immediately when the average temperature of the air drops below the lake bottom temperature [Zdorovennova, 2009].

[15] We examine the periodicity of the temperature F5 records by spectral analysis (Figure 5a). The amplitude spectrum of the temperatures shows few pronounced maxima at 24.0, 12.1, and 8.0 h. While the 24 h period is undisputable, we consider the relevance of the 8 and 12 h periods questionable. The reason is the spiky character of the temperature records caused by the insufficient amplitude resolution of the digitized temperature, which generates higher harmonics.

### Discussion 4.

[16] Two possible physical mechanisms are considered that could be responsible for periodical discharge of the



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Figure 5. Amplitude spectra show (a) temperature and (b) barometric records at depths of 22 and 30 cm for the period 20 January to 10 February 2011 when the amplitude of 603 oscillations was the highest.

607 warmer water to the lower part of the measured profile. The 608 first are the basin-scale internal waves that may affect the temperature distribution in shallow lakes. Among them, two kinds of waves can be distinguished. The first are the 610611 baroclinic seiches. The period of a baroclinic seiche is given [Gill, 1982; Zdorovennova, 2009] as

$$T_1 = \frac{2\pi L}{H\sqrt{\frac{g}{\rho}\frac{d\rho}{dz}}},$$
 (4)  $\begin{array}{c} 614\\ 615\\ 616\end{array}$ 

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where the index 1 denotes mode of the baroclinic seiche, L618 is the maximum length of the lake basin, H is the mean 619 depth of the lake minus the ice thickness, g is the gravity 620 acceleration,  $\rho$  is the average water density, and its deriva-621 tive is average vertical density gradient. 622

[17] Another kind of basin-scale internal waves is con-623 nected with inertial frequency and the Earth rotation, which 624 generate waves of the geostrophic inertia-gravity character 625 of two frequencies [Kirillin et al., 2009] split around the 626 inertia-gravity waves into supercritical (Poincare wave) 627 and subcritical (Kelvin wave) modes propagating in oppo-628 site directions [Gill, 1982]. Kelvin wave affects the water-629 sediment interface in the littoral zone, where it can produce 630 shear turbulence and resuspension, while the Poincare 631 wave produces water movements in the middle of the lake 632 [Kirillin et al., 2009]. Dissipation of these rotational waves 633 has longer time scales than simple seiches and for elliptical 634 basin can last up to 1 week [Antenucci and Imberger, 635 2001a, 2001b]. 636

[18] The second mechanism is the tidal accelerations that 637act on both the solid Earth and water bodies, generating 638 time-dependent changes of the water level. The combina-639 tion of the Moon and Sun motions with the Earth rotation 640

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results in a complex time dependence of tidal acceleration, 643 which can be expressed as a sum of harmonic tidal constit-644 uents with prevailing diurnal and semidiurnal periods. 645 Unlike the oceans, the groundwater is not attracted directly 646 by the tidal forces. Instead, the solid Earth tides generate 647 deformation of the rock environment, which results in 648 cyclic opening and closing of the pore space [Fischer et al., 649 2006; Rojstaczer and Riley, 1990]. It results in oscillations 650 of pressure head causing Darcian flow of groundwater that 651 periodically changes its direction. 652

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[19] For the selection of the more likely mechanism we 653 first verify the possible effect of seiches by examining their 654 period, which depends on the lake geometry and density 655 gradients. Using approach of Zdorovennova [2009], the pe-656 riod of a baroclinic seiche can be evaluated using equation 657 F6 (4). In Figure 6 we show the dependence of seiche period 658 659 on the bottom temperature and mean lake depth for the maximum length of the lake basin L = 1.5 km and average 660 water density  $\rho = 999.957$  kg/m<sup>3</sup>. Average water density 661 gradient was estimated from the bottom and ice interface 662 temperatures, and the lake depth H was considered in the 663 range 0.5–2.5 m. It appears that if for the bottom tempera-664 ture ranges from 0°C to 4°C the seiche period varies from 665 about 2 days and more. However, the bottom temperature 666 probably does not exceed 1° C based on the measured tem-667 perature profile and the mean lake bottom temperatures 668 measured in Minnesota [Fang and Stefan, 1998]. There-66AQ4 fore, the seiche period would exceed 3 days, which is in 670 contrast with the exact period of the temperature oscilla-671 tions of 24 h found in the spectrum in Figure 5a. This dis-672 qualifies the seiches as the possible driving force and 673 674 supports tides as the most likely driving mechanism of 675 observed temperature variations.

[20] Next we analyze the possible influence of tides. The mechanism that could convert the tidal acceleration to the



Figure 6. Period of baroclinic seiches as a function of bottom temperature and lake depth (equation (4)) calculated for L = 1.5 km and temperature-dependent water density. The bold line refers to the mean depth of the lake of 1.7 m.

oscillations of pressure head may be complex as it strongly depends on the structure of the underlying layers, particularly in the presence of fractures and/or faults. Such mechanisms were presented in mathematical models [Bodvarss, 1970; Ondovcin et al., 2012]. In our approach we assume a presence of semipervious aquitard beneath the lake bottom. Lake sediment layer does not allow for any measurable amount of flow through the whole surface of the bottom. However, the communication between the underlying aquifer and the lake water is possible through preferential zones. As the water enters the lake bottom via these zones, it spreads laterally over the lake's floor due its higher density, while the heat in vertical direction moves conductively.

[21] For tidal analysis of periodic inflow of groundwater we compared the theoretical Earth tides with the temperature records. We have evaluated the tidal effects for the region of interest in Minnesota at latitude 45.201°N and longitude -93.504°E. The ocean load was not taken into account because of its negligible effect at a distance larger than 1000 km from the sea. The tidal potentials and the vector tidal acceleration for the investigated time period were calculated using a program [Skalsky, 1990] based on Tamura's [Tamura, 1987] development. Additionally, the volumetric strains and the longitudinal strains in the N, E, and Z directions were evaluated using a slightly modified ETERNA program [Wenzel, 1993] based on the global elastic tide model. The selected tidal characteristics are shown along with the temperature records in Figure 7 and F735 indicate a possible relationship between the temperature data and the modeled solid Earth tides. To quantify this relation a cross correlation of the time series in the time lag interval from -4 to +4 days was determined (Figure 8). In F839 terms of the tidal force, the maximum cross correlation of 0.49 at the phase lag of 50 h and the maximum anticorrelation of -0.44 at the lag of -10 h were found for the vertical component of the tidal force. The solid Earth strains show the maximum correlation of 0.45 for the phase lag of about 9 h and maximum anticorrelation of -0.44 for the phase lag of 21 h. Here the positive phase lag corresponds to a delay of the temperature maxima after the maxima of the Earth tides.

748 [22] The cross-correlation factor of about 0.4 is not insig-749 nificant, namely, in view of the spiky temperature record, 750 which ranges within the first digits of the sensors' tempera-751 ture resolution of 0.06°C. Note that the cross correlation 752 with tides shows global maxima within the interval of 0-2 753 days (Figure 8). Especially, the tidal force shows sharp 754 global maximum. This suggests that both the daily period 755 and the low-frequency modulation period present in Earth 756 tides are transferred to the temperature oscillations. The 757 similar values of positive correlation and anticorrelation for 758 both the vertical component of the tidal force and for the 759 volumetric tidal strains do not allow for clear identification 760 of the driving mechanisms of the temperature variations. 761 The fact that the temperature maxima follow the maxima 762 of the Earth tides with a delay of several hours supports the 763 hypothesis that the groundwater is injected from the under-764 lying aquifer due to the tidal effects. 765

[23] In addition to the Earth tides acting as a driving 766 force for periodic temperature variations, the effect of 767 atmospheric tides also should be examined. In contrast to 768

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**Figure 7.** Detailed segment of all of the temperature data from 10 data loggers and Earth tides for the period 18–26 December 2010. Solid line is the vertical component of tidal acceleration, and dashed line is the volume strain. The numbers in the legend are the depths of the sensors underneath the water level in centimeters.

Earth tides, the atmospheric tides are driven by periodic solar heating of the atmosphere with a strongly prevailing 12 h period [*Chapman and Lindzen*, 1970; *Covey et al.*, 2011] as the influence of the equator region dominates. Despite the fact that the tidal variations at middle latitudes are masked by air pressure variations due to weather changes [*Lindzen and Chapman*, 1969], the 12 h period is present in the spectrum of Figure 5 for the barometric pressure record in Minnesota (compare the long-period variations dominating the barometric record in Figure 2 with its spectrum in Figure 5). We infer that the influence of atmospheric tides



**Figure 8.** Cross-correlation function between volumetric strain and temperature. Positive phase corresponds to delay of temperature at 30.5 cm depth after Earth tides (tidal force, dashed line; volumetric strain, full line) for the observational period shown in Figure 7.

is negligible because their dominant period of 12 h vanishes in the temperature records where 24 h period dominates.

[24] The water table fluctuation due to Earth tides is a complex function of the hydraulic parameters of the aqui-fers. Larger fluctuations are expected if the formation has a higher permeability and a lower specific yield [Rojstaczer and Riley, 1990]. This could be the case of the investigated area, whose surficial geology includes silt containing till with specific yield typically below 10% [Johnson, 1967]. It should be noted that many observations show that the tidal behavior of wells is strongly laterally dependent [Mrlina et al., 2003]. Such dependence could be caused by a lateral heterogeneity of the aquifer whose parts are connected with a deeper fault system that is exposed to a cyclic stress per-turbation due to the Earth tides. 

### 5. Conclusions

[25] Analysis of the vertical profile of the lake water temperatures for a period of 3 months during the winter shows that water temperature under the ice oscillates by 0.2°C with a daily period, while the temperature of the ice shows only the long-period changes reflecting the variation of the air temperature. The temperature variation from shal-low to deeper parts of the lake is governed by the periodic thermal conduction during the first month. However, during the second and the third month we identified the existence of the periodic variable insulation condition responsible for variable heat conduction at the ice-water interface and sharp deviation from regular periodic heat conduction observed during the first month. 

[26] We have provided two models explaining the periodic thermal oscillation near the lake ice-water interface. 894 The first model is considering the baroclinic seiches. Specific lake geometry indicates the period of the first mode of 896

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barometric seiches is larger than 3 days, which is far from what we observed. The second model, the influence of Earth tides, appears more consistent with the data because the temperature period matches the 1 day period the Earth tides.

[27] We propose that the Earth tides may periodically change the porosity of the underlying aquifer, squeezing periodically the warmer water out toward the surface. This process would be responsible for the water temperature variations by the periodic inflow of the warmer groundwater. Because the water stays below the 4°C at the lake bottom, the heat is transferred by conduction, which we confirmed by comparing the measured data with the theoretical model. The tidal influence on lake temperature oscillation is supported by both spectral analysis of tides and cross correlation of measured temperature series with the modeled tidal force and volumetric strains.

[28] Observations of the tide and/or baroclinic seicheinduced temperature changes have yet not been reported and open an important angle when estimating the thermal budget under the lake ice. These changes speed up the transfer of heat from the bottom to the ice cover and serve as an important variable for existence of life in completely covered water bodies with ice (Lake Vostok) or similar once on other planets (Mars) and moons (Europa).

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