

# **Multivariační metody v taxonomii**

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**prezentácie dostupné na:**

**<https://botany.natur.cuni.cz/brassiploidy>**

**Fenetický prístup** (multivariačné metódy; “pattern”; zhluková analýza, ordinačné metódy, diskriminačná analýza)

**Kladistický prístup** (parsimonická analýza)

**Alternatívne prístupy** k rekonštrukcii fylogenézy  
(metóda spájania susedných objektov – *neighbour joining method*; metódy najväčšej pravdepodobnosti – *maximum likelihood*; Bayesovské metódy – *Bayesian statistical methods*)

**Geometrická morfometrika** (Booksteinove súradnice tvaru, Prokrustova analýza, metóda ohybných pásiek - *thin plate spline*)

**Softvér:** MorphoTools2, SYN-TAX 2000,  
[PAUP\* version 4.0, beta version 10 (<http://paup.csit.fsu.edu/>),  
ďalší špecializovaný softvér]

# Fenetický prístup

Michel Adanson (1727-1806)

*Familles des Plantes* (1763)

65 rôznych klasifikácií,  
založených vždy na jednom  
znaku (napr. placentácia, typ  
súkvetia ...)

**P R E F A C E**

|                               |                               |                               |                     |
|-------------------------------|-------------------------------|-------------------------------|---------------------|
| 35. Bignon.                   | 12. Q. Pourpier.              | 10. Orchis.                   | 21. P. Chevreuille. |
| <b>17<sup>e</sup> CLASSE.</b> | 42. Q. Rosier.                | 11. Aristoloches.             | 12. M. Avelin.      |
| <i>Etamines sur le</i>        | <b>18<sup>e</sup> CLASSE.</b> | <b>20<sup>e</sup> CLASSE.</b> | 23. Apocins.        |
| <i>Calice &amp; sur</i>       | <i>Etamines sur</i>           | <i>Etamines sur la</i>        | 24. Bouraches.      |
| <i>l'Overe ensem-</i>         | <i>l'Overe.</i>               | <i>Corole.</i>                | 25. Labiées.        |
| <i>ble.</i>                   | 9. 6. Jousabres.              | 9. 10. Jousabres.             | 26. Verrées.        |
| 13. Eleagout.                 | 11. 11. Aristoloches.         | 16. Composées.                | 27. Perforées.      |
| 15. Onagres.                  | <b>19<sup>e</sup> CLASSE.</b> | 17. Campanules.               | 28. Solanons.       |
| 14. Mirtes.                   | <i>Etamines sur le</i>        | 18. Bignon.                   | 29. Jasmens.        |
| 19. Umbellifères.             | <i>fil de l'Overe.</i>        | 19. Apocins.                  | 30. Anagallis.      |
| 22. Chevreuille.              |                               | 20. Scabieuses.               | 31. Q. Pourpier.    |
|                               |                               |                               | 32. Q. Jousabres.   |
|                               |                               |                               | 34. Q. Allines.     |

42. *Système. Etamines; leur figure respective.*

|                               |                     |                              |                              |
|-------------------------------|---------------------|------------------------------|------------------------------|
| <b>1<sup>re</sup> CLASSE.</b> | 11. Chevreuilles.   | <b>3<sup>e</sup> CLASSE.</b> | <b>5<sup>e</sup> CLASSE.</b> |
| <i>Plantes sans Et-</i>       | 12. Avelin.         | <i>Etamines réunies</i>      | <i>Etamines réunies</i>      |
| <i>amines.</i>                | 23. 26 Apocins.     | <i>toutes ensemble</i>       | <i>par les filets en</i>     |
| 1. Bignon.                    | 24. Bouraches.      | <i>par les filets en</i>     | <i>plus de 2 corps.</i>      |
| 2. Champignons.               | 25. Labiées.        | <i>un faisceau.</i>          | 41. 2. Légumineux.           |
| 3. 6. Fucus.                  | 26. Verrées.        |                              | 52. 1. Crucifères.           |
|                               | 27. Perforées.      |                              | 34. 7. Cistes.               |
| <b>2<sup>e</sup> CLASSE.</b>  | 12. 9. Solanons.    | 3. 3. Fucus.                 |                              |
| <i>Etamines diffé-</i>        | 29. Jasmens.        | 6. Palmiers.                 | <b>6<sup>e</sup> CLASSE.</b> |
| <i>rent les uns des</i>       | 30. Anagallis.      | 8. 2. Liliacés.              | <i>Etamines réunies</i>      |
| <i>autres.</i>                | 31. Salicées.       | 11. 2. Aristoloches.         | <i>par les anteres</i>       |
|                               | 32. Pourpier.       | 76. Jalaps.                  | <i>seulement.</i>            |
|                               | 33. Jousabres.      | 37. Amaroques.               |                              |
|                               | 34. Allines.        | 42. Esquagout.               |                              |
|                               | 35. Bignon.         | 43. 26. Légumineux.          |                              |
|                               | 39. Ferrières.      | 44. 16. Pistachiés.          |                              |
|                               | 40. Carou.          | 41. 11. Titimalés.           |                              |
|                               | 41. Rosiers.        | 49. Geranions.               | 16. 112. Composées.          |
| 4. Epurées.                   | 42. Jujubiés.       | 50. Mauves.                  | 17. 3. Campanules.           |
| 5. Fougères.                  | 43. 22. Légumineux. | 51. Capriés.                 | 18. 13. Bignon.              |
| 7. Gramens.                   | 44. 16. Pistachiés. | 57. Pins.                    | 21. 2. Apocins.              |
| 8. 72. Liliacés.              | 45. 12. Titimalés.  |                              | 22. 1. Solanons.             |
| 9. Jousabres.                 | 46. Anons.          | <b>4<sup>e</sup> CLASSE.</b> | 33. 1. Pavot.                |
| 10. Orchis.                   | 47. Chevreilles.    | <i>Etamines réunies</i>      |                              |
| 11. 11. Aristoloches.         | 48. Tillés.         | <i>par les filets en</i>     |                              |
| 12. Eleagout.                 | 32. 42. Crucifères. | <i>3 corps.</i>              | <b>7<sup>e</sup> CLASSE.</b> |
| 13. Onagres.                  | 33. 16. Pavots.     |                              | <i>Etamines réunies</i>      |
| 14. Mirtes.                   | 34. 64. Cistes.     |                              | <i>par les filets &amp;</i>  |
| 19. Umbellifères.             | 35. 11. Renouées.   |                              | <i>les anteres en</i>        |
| 26. 6. Composées.             | 36. Aross.          |                              | <i>semble.</i>               |
| 27. 6. Campanules.            | 38. Mousés.         | 45. 61. Légumineux.          |                              |
| 18. 1. Bignon.                |                     |                              |                              |
| 19. Apocins.                  |                     |                              |                              |
| 20. Scabieuses.               |                     |                              |                              |

23. 2. Apocins.

## Fenetický prístup

Department of Entomology, University of Kansas, Lawrence, U.S.A.

Michener, Ch.D. & Sokal, R.R. 1957. A quantitative approach to a problem in classification. *Evolution* 11: 130-162.

Department of Microbiology, University of Leicester, U.K.

Sneath, P.H.A. 1957. Some thoughts on bacterial classification. *J. Gen. Microbiol.* 17: 184-200.

Sokal, R.R. & Sneath, P.H.A. 1963. *Principles of numerical taxonomy*. W. H. Freeman and comp., San Francisco & London.

Sneath, P.H.A. & Sokal, R.R. 1973. *Numerical taxonomy, the principles and practice of numerical classification*. W. H. Freeman and comp., San Francisco.

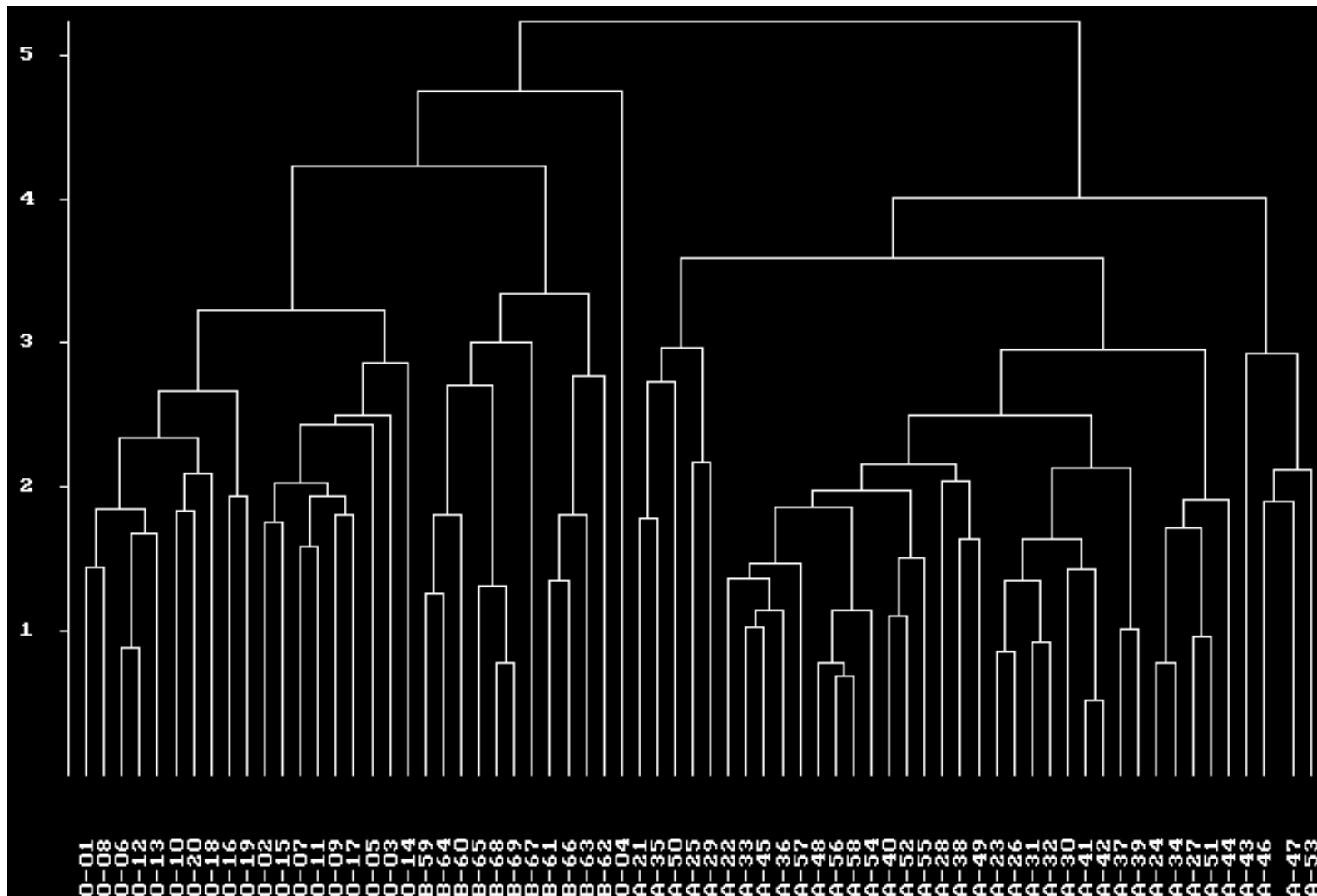
## Neo-adansonovské princípy

- Čím väčší je **obsah informácie** v taxónoch a na čím väčšom počte znakov je klasifikácia založená, tým je táto klasifikácia lepšia.
- Každý **znak** má pri tvorbe taxónov **rovnakú váhu**.
- Celková **podobnosť** medzi akýmkoľvek dvomi jednotkami je funkciou podobností v jednotlivých znakoch.
- Taxóny sa rozoznávajú na základe toho, že sa **korelácie** medzi znakmi v rôznych skupinách líšia.
- **Úsudky o fylogénéze** sa môžu robiť z taxonomickej štruktúry skupiny a z korelácií medzi znakmi. Berú sa pritom do úvahy určité predpoklady (premisy) o evolučných cestách a mechanizmoch.
- Taxonómia sa považuje za **praktickú a empirickú vedu**.
- Klasifikácie sa zakladajú na **empirickej podobnosti**.

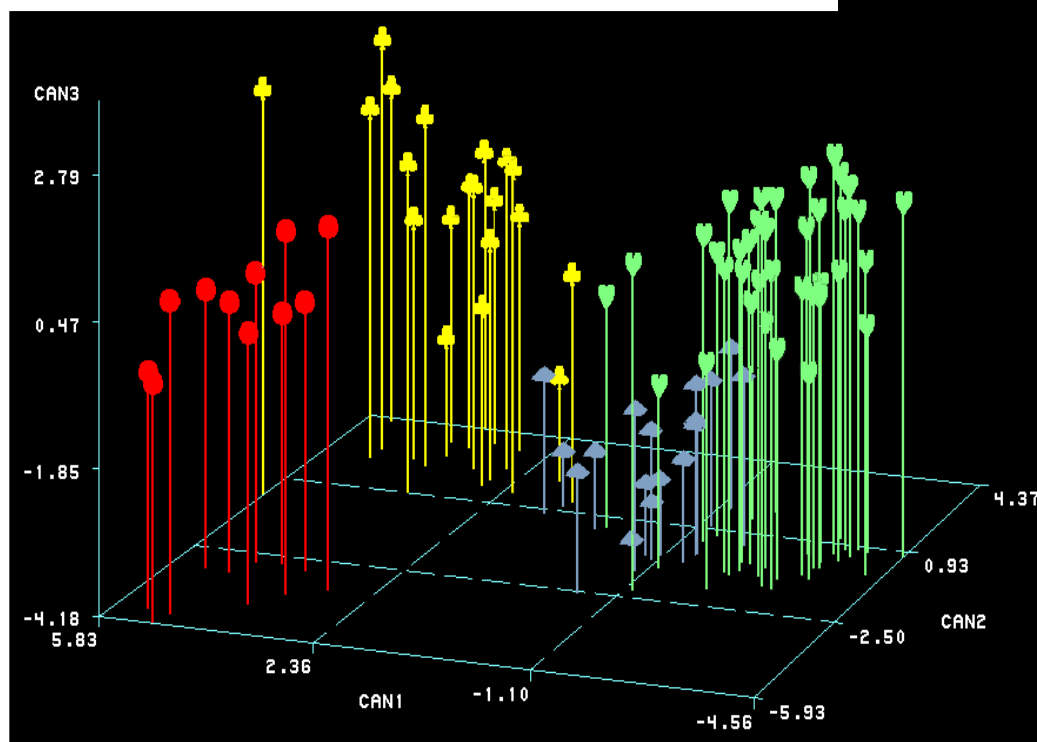
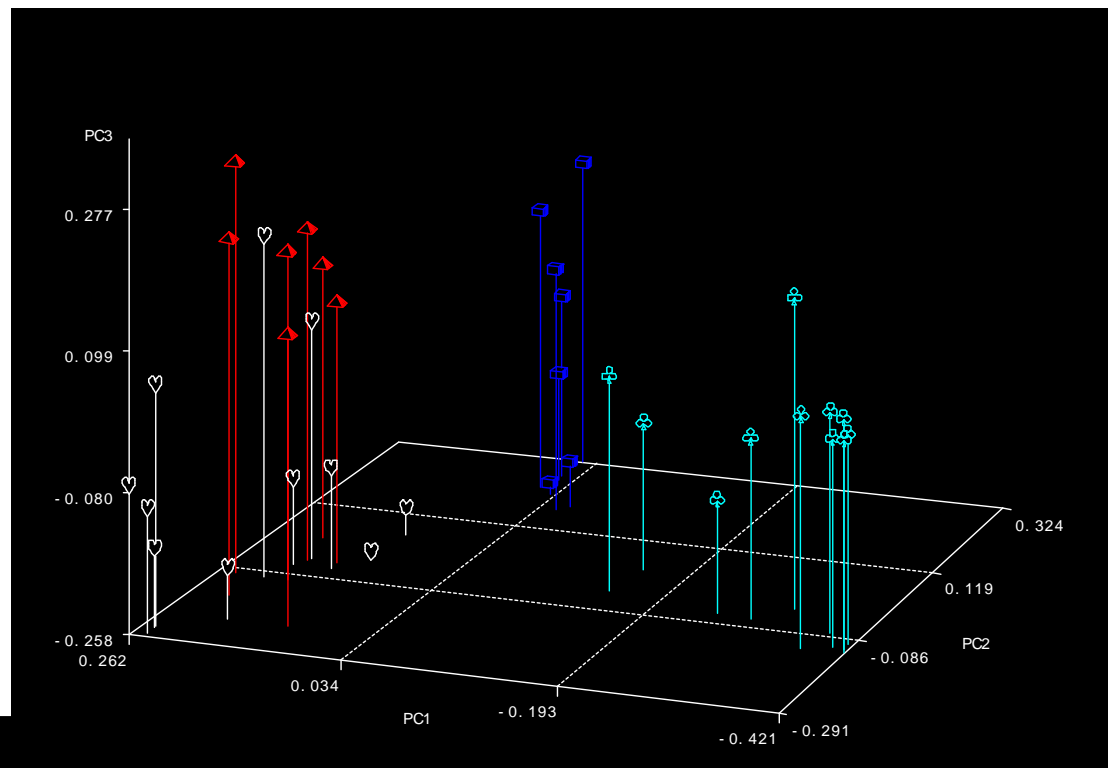
# Fenetický prístup

- Termíny: numerical taxonomy (Sokal & Sneath), statistical systematics (Solbrig), numerical phenetics (Duncan & Baum), multivariate morphometrics (Blackith & Reyment)
- Operačné taxonomické jednotky (OTU)
- Znaky, primárna matica, počet znakov, korelácie
- Koeficienty vyjadrujúce vzťahy medzi znakmi alebo objektmi, sekundárna matica
- Multivariačné metódy (zhlukovacie metódy, ordinačné metódy, diskriminačná analýza)
- Rôzne metódy môžu priniesť rôzne výsledky
- Využitie metód v minulosti a v súčasnej taxonomickej praxi (infrašpecifická variabilita, polyploidné komplexy, štúdium morfolologickej variability v rozsiahlych areáloch, molekulárne dáta)

# Zhlukovacia analýza



# Analýza hlavných komponentov



Kanonická  
diskriminačná analýza

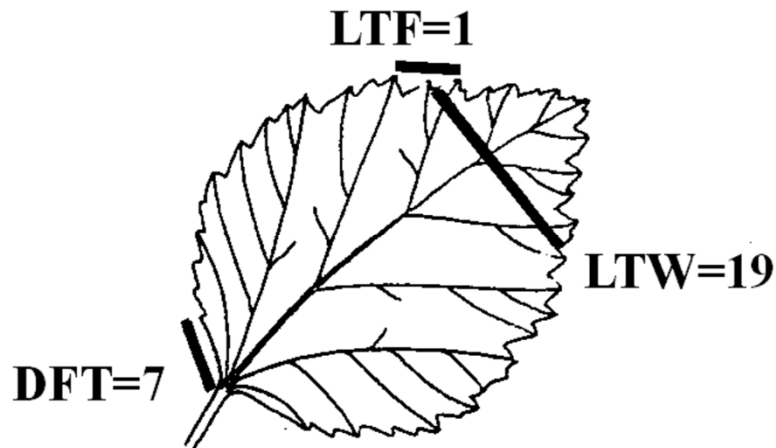


## Klasifikačná diskriminačná analýza

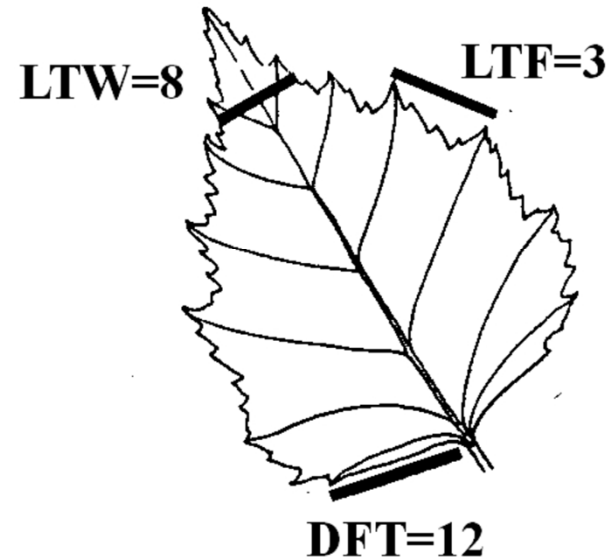
skupina                      príslušnosť rastlín k stanoveným skupinám predpovedaná na základe vytvoreného klasifikačného kritéria (absolútny počet a percento rastlín klasifikovaných do jednotlivých skupín)

|                  | <b>amara</b> | <b>austr.</b> | <b>olot.</b> | <b>opicii</b> | <b>pyren.</b> | <b>Celkom</b> |
|------------------|--------------|---------------|--------------|---------------|---------------|---------------|
| <b>amara</b>     | <b>349</b>   | 20            | 3            | 1             | 7             | 380           |
|                  | <b>91.84</b> | 5.26          | 0.79         | 0.26          | 1.84          | 100.00%       |
| <b>austrica</b>  | 51           | <b>302</b>    | 1            | 6             | 8             | 368           |
|                  | 13.86        | <b>82.07</b>  | 0.27         | 1.63          | 2.17          | 100.00%       |
| <b>olotensis</b> | 2            | 0             | <b>99</b>    | 0             | 0             | 101           |
|                  | 1.98         | 0.00          | <b>98.02</b> | 0.00          | 0.00          | 100.00%       |
| <b>opicii</b>    | 1            | 9             | 0            | <b>326</b>    | 42            | 378           |
|                  | 0.26         | 2.38          | 0.00         | <b>86.24</b>  | 11.11         | 100.00%       |
| <b>pyrenaea</b>  | 1            | 11            | 0            | 19            | <b>207</b>    | 238           |
|                  | 0.42         | 4.62          | 0.00         | 7.98          | <b>86.97</b>  |               |

*B. pubescens* = -35



*B. pendula* = +21



**Diskriminačná funkcia** na určenie druhov *Betula pubescens* a *B. pendula*

$12LTF + 2DFT - 2LTW - 23$

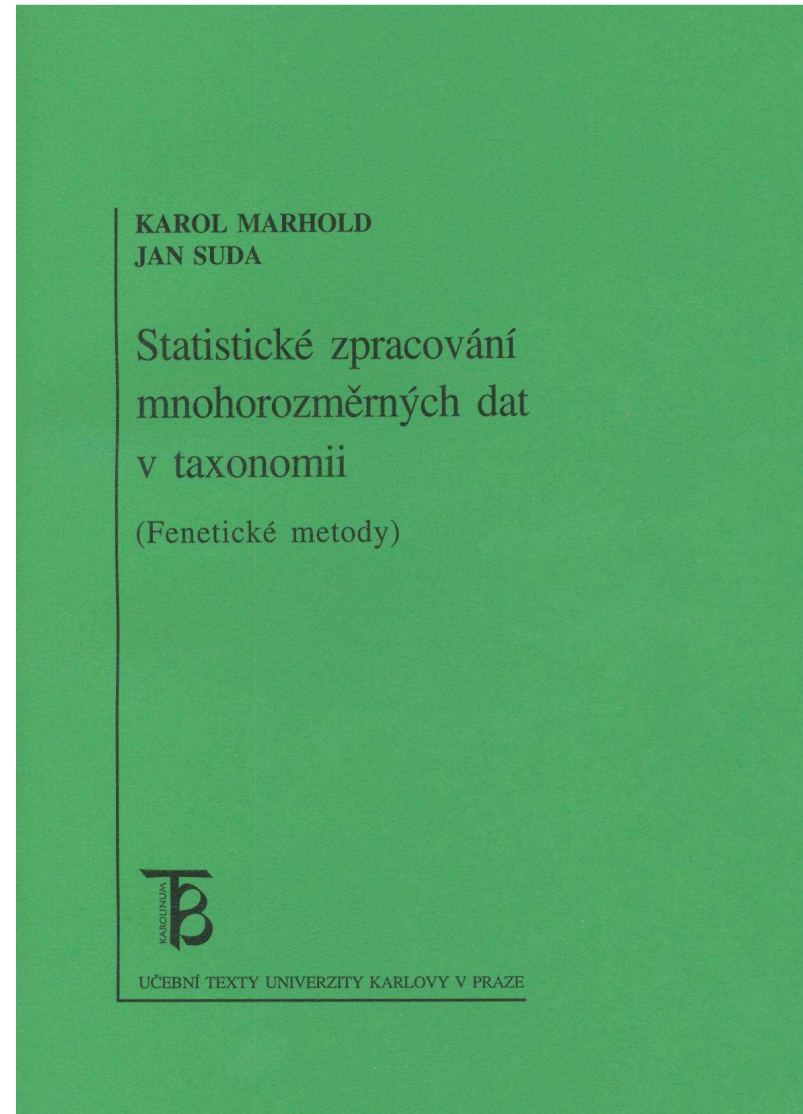
kladné hodnoty *B. pendula*

záporné hodnoty *B. pubescens*

pravdepodobnosť správneho určenia 93%

(Stace, C. A., 1991, New Flora of the British Isles)

Marhold, K. & Suda, J. 2002: *Statistické zpracování  
mnohorozměrných dat v taxonomii*. Karolinum, Praha.

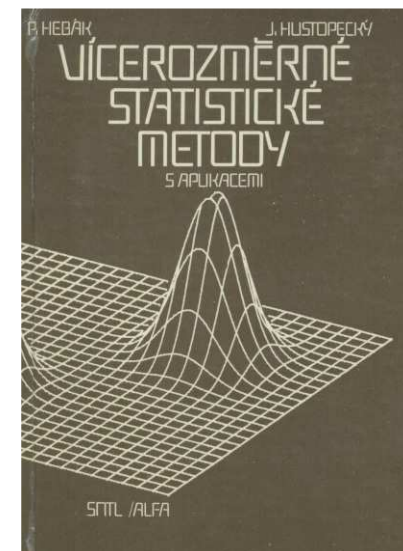


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Hebák, P., Hustopecký, J., Jarošová, E. & Pecáková, I. 2007. *Vícerozměrné statistické metody (1)*. Ed. 2. Informatorium, Praha.

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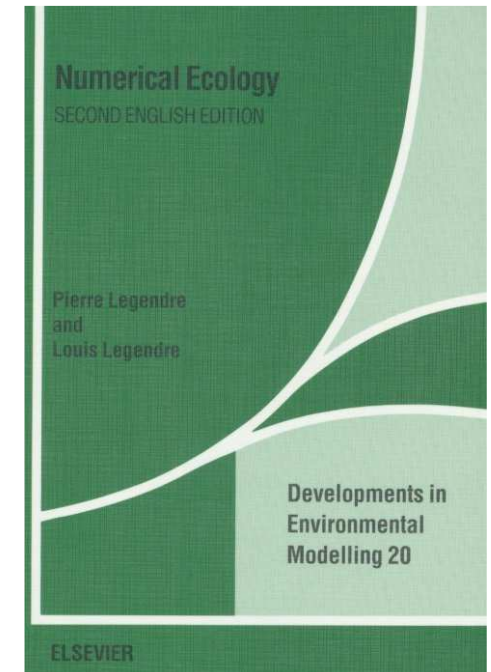
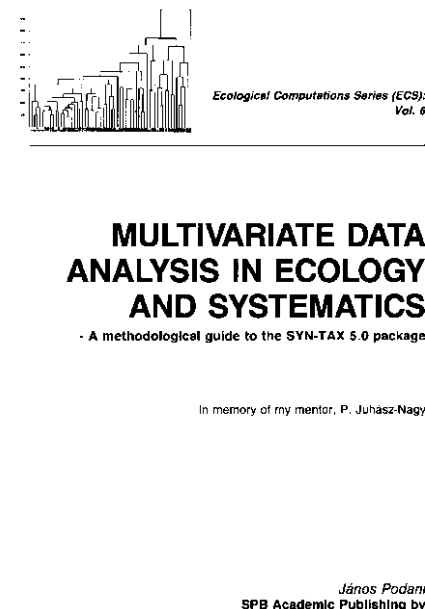
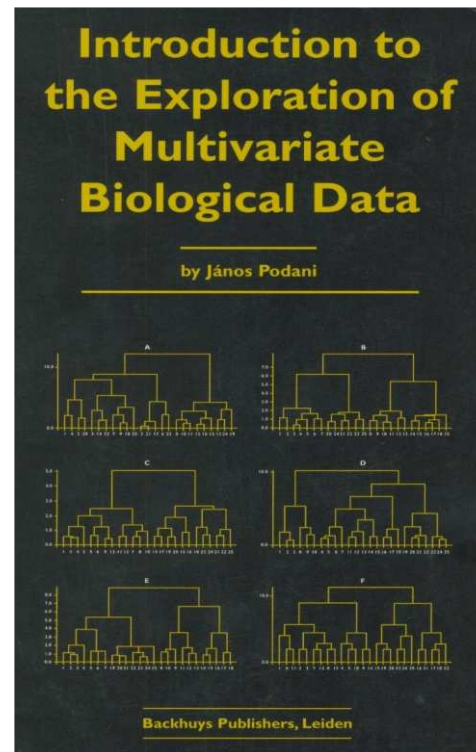
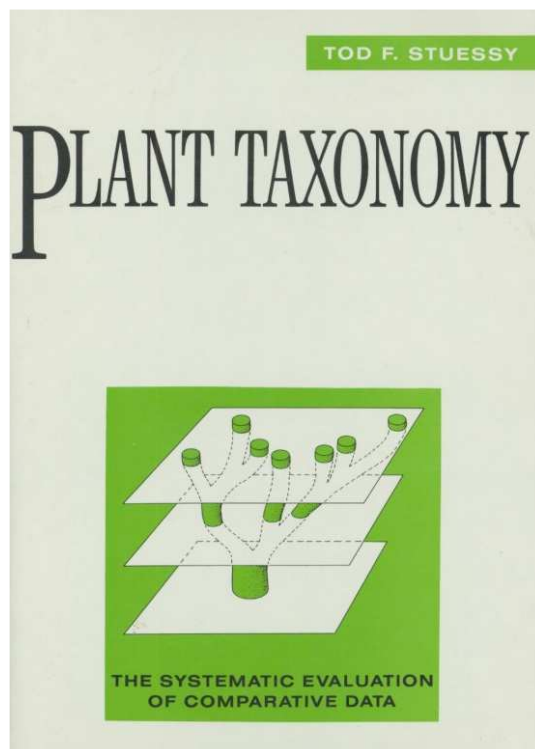


Legendre, P. & Legendre, L. 1998. *Numerical ecology*. Second English edition. Elsevier, Amsterdam.

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Podani, J. 2000. *Introduction to the exploration of multivariate biological data*. Backhuys Publishers, Leiden.

Stuessy, T. F. 1990. *Plant taxonomy: the systematic evaluation of comparative data*. Columbia University Press, New York.



## Kladistický prístup

### Hennig, W.

**1950:** *Grundzüge einer Theorie der phylogenetischen Systematik*. Deutsche Zentralverlag, Berlin.

**1965:** Phylogenetic systematics. *Annual Review of Entomology* 10: 97-116.

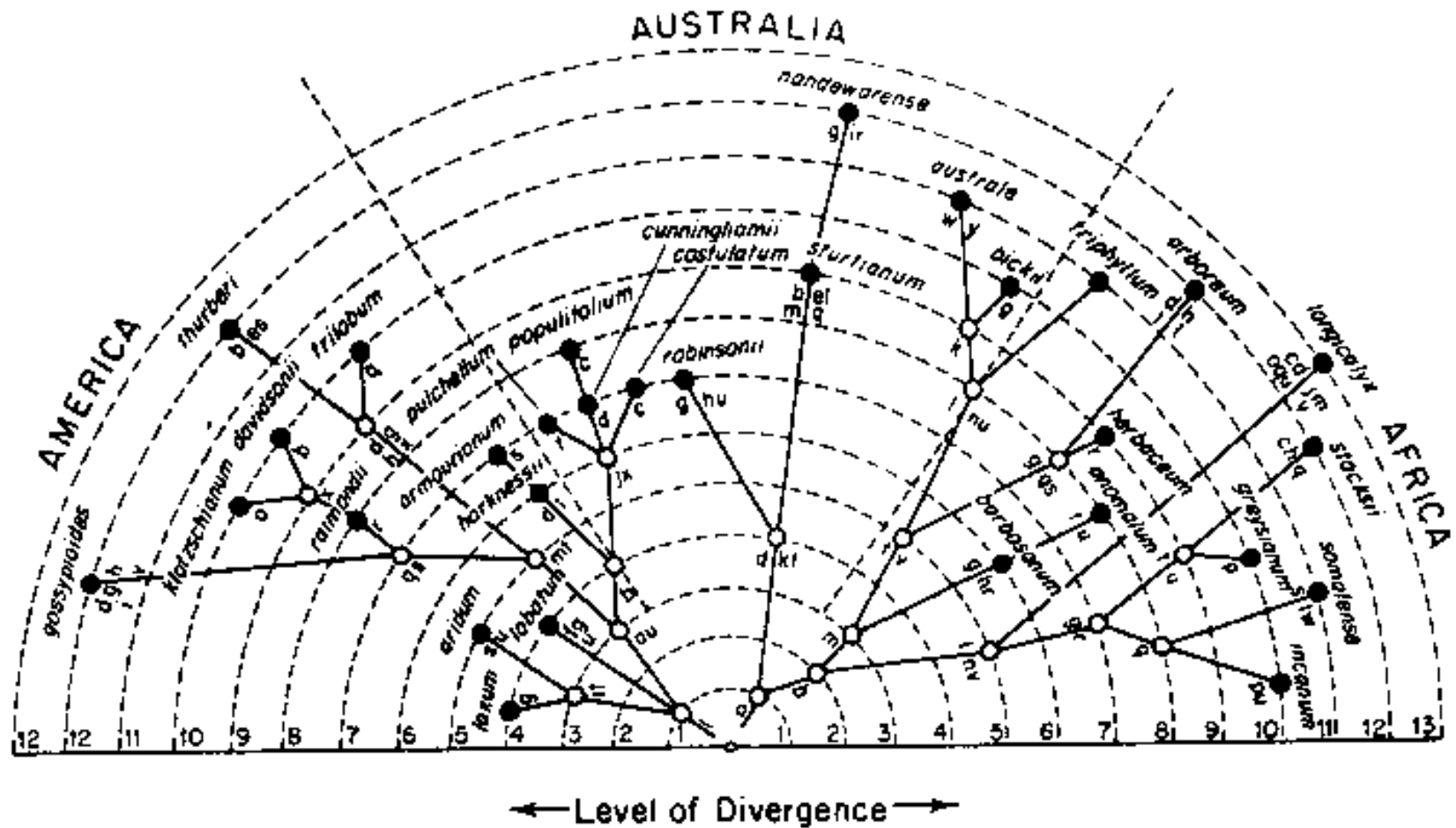
**1966:** *Phylogenetic systematics*. University of Illinois Press, Urbana.

### Botanika:

Koponen, T., 1968: Generic revision of Mniaceae Mitt. (Bryophyta). *Ann. Bot. Fenn.* 5: 117-151.

Funk, V. & Stuessy, T. F. 1978: Cladistics for practicing plant taxonomist. *Syst. Bot.* 3: 159-178.

Bremer, K. & Wantorp, H.- E. 1978: Phylogenetic systematics in botany. *Taxon* 27: 317-329.



**Fig. 2.17** Cladogram (Wagner tree) of 30 species of *Gossypium* (Malvaceae), modified from Frywell<sup>142</sup>.

W.H. Wagner, University of Michigan - Groundplan/divergence method

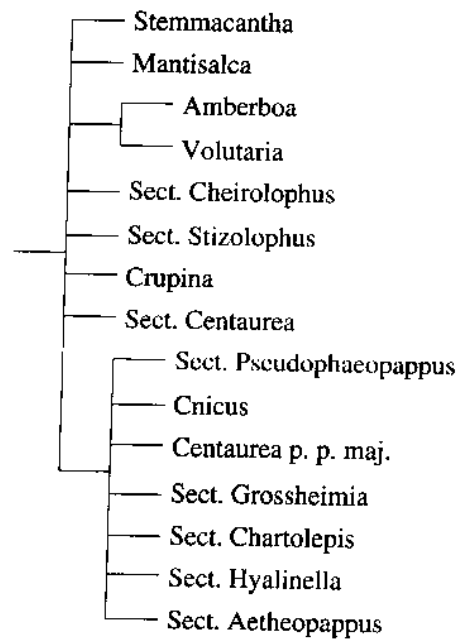


FIGURE 8-4. Strict consensus tree of six equally parsimonious cladograms of *Centaurea* sections and related genera based on cypselae characters from Dittrich (1966, pp. 138–139). The data matrix is given in Table 8-4.

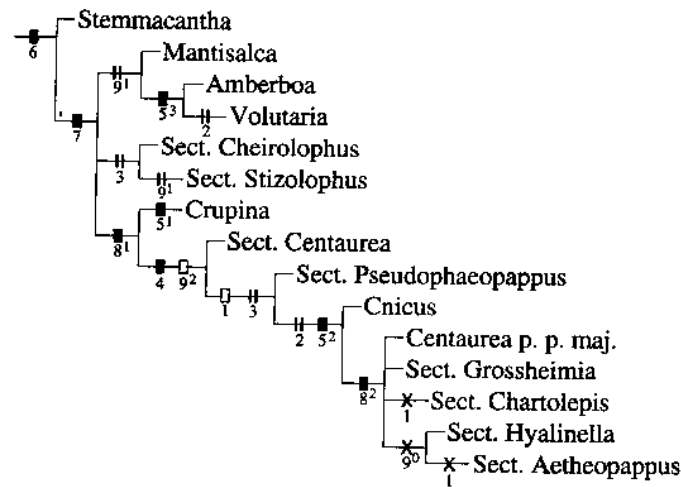


FIGURE 8-5. One of six equally parsimonious cladograms of *Centaurea* sections and related genera based on cypselae characters from Dittrich (1966, pp. 138–139). The characters are given in Table 8-3 and the data matrix in Table 8-4. Solid bars indicate nonhomoplastic synapomorphies; open bars indicate homoplastic synapomorphies with reversals; double bars indicate parallelisms; crosses indicate reversals.

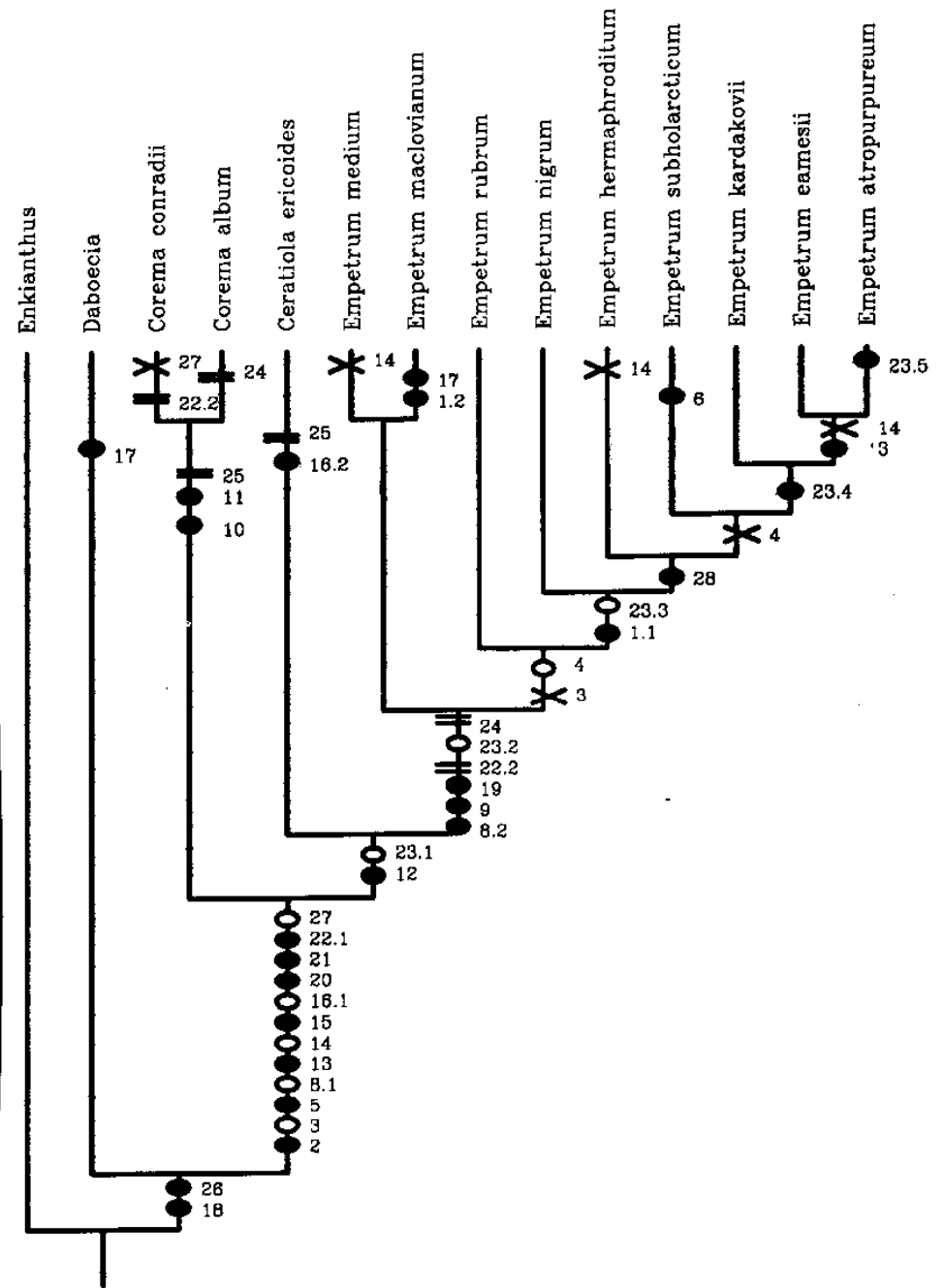
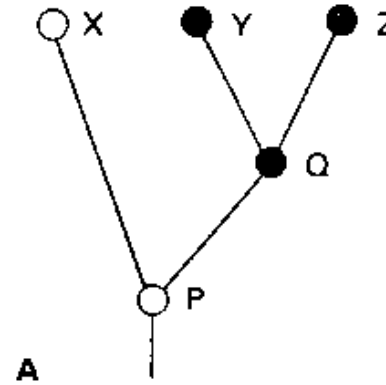


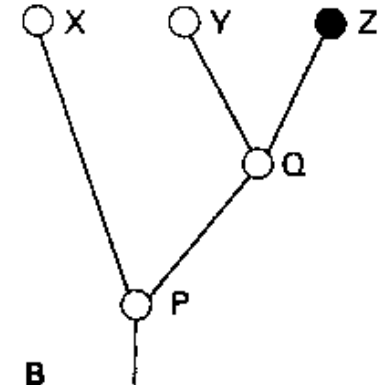
FIG. 2. One of five equally parsimonious cladograms of the Empetraceae. *Enkianthus* and *Daboecia* are outgroup taxa. Characters are numbered in accordance with the text, Appendix 1, and with Table 1. Black dots = synapomorphies (ci = 1), white dots = synapomorphies (ci < 1), parallel lines = parallelisms, crosses = reversals.



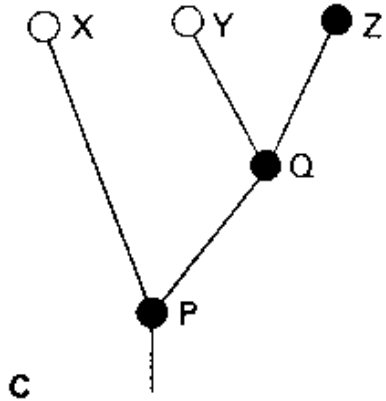
**A** Y-Z, X-Y-Z  
monofyletické skupiny



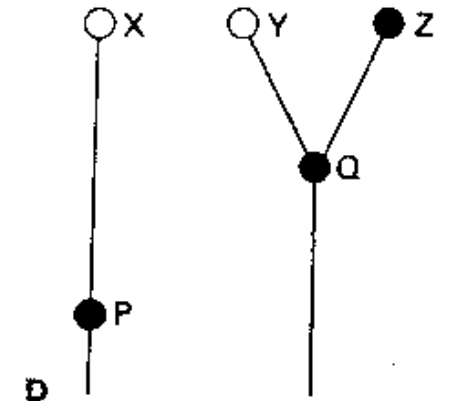
**B** X-Y parafyletická  
skupina



**C** X-Y polyfyletická  
skupina, paralelizmus



**D** X-Y polyfyletická  
skupina, konvergencia



**Fig. 2.6** Four diagrams showing different origins of three species (X, Y, Z) from the ancestral taxa P and Q in order to illustrate the concepts of monophyly, paraphyly, polyphyly, parallelism and convergence. The possession of one or other of two contrasting character-states by each of the five taxa is indicated by an open or closed circle respectively. **A.** Groups YZ and XYZ are both monophyletic; the similarity between Y and Z is a synapomorphy; the difference between X and YZ is due to divergence. **B.** Group XY is paraphyletic; group XYZ is monophyletic; the similarity between X and Y is a symplesiomorphy; the difference between Y and Z is due to divergence. **C.** Group XY is polyphyletic; group XYZ is monophyletic; the similarity between X and Y is a false synapomorphy caused by parallelism. **D.** Groups XY and XYZ are both polyphyletic; group YZ is monophyletic; the similarity between X and Y is a false synapomorphy caused by convergence.

## **Primitívny stav znaku**

Pleziomorfia

Sympleziomorfia

## **Odvođený stav znaku**

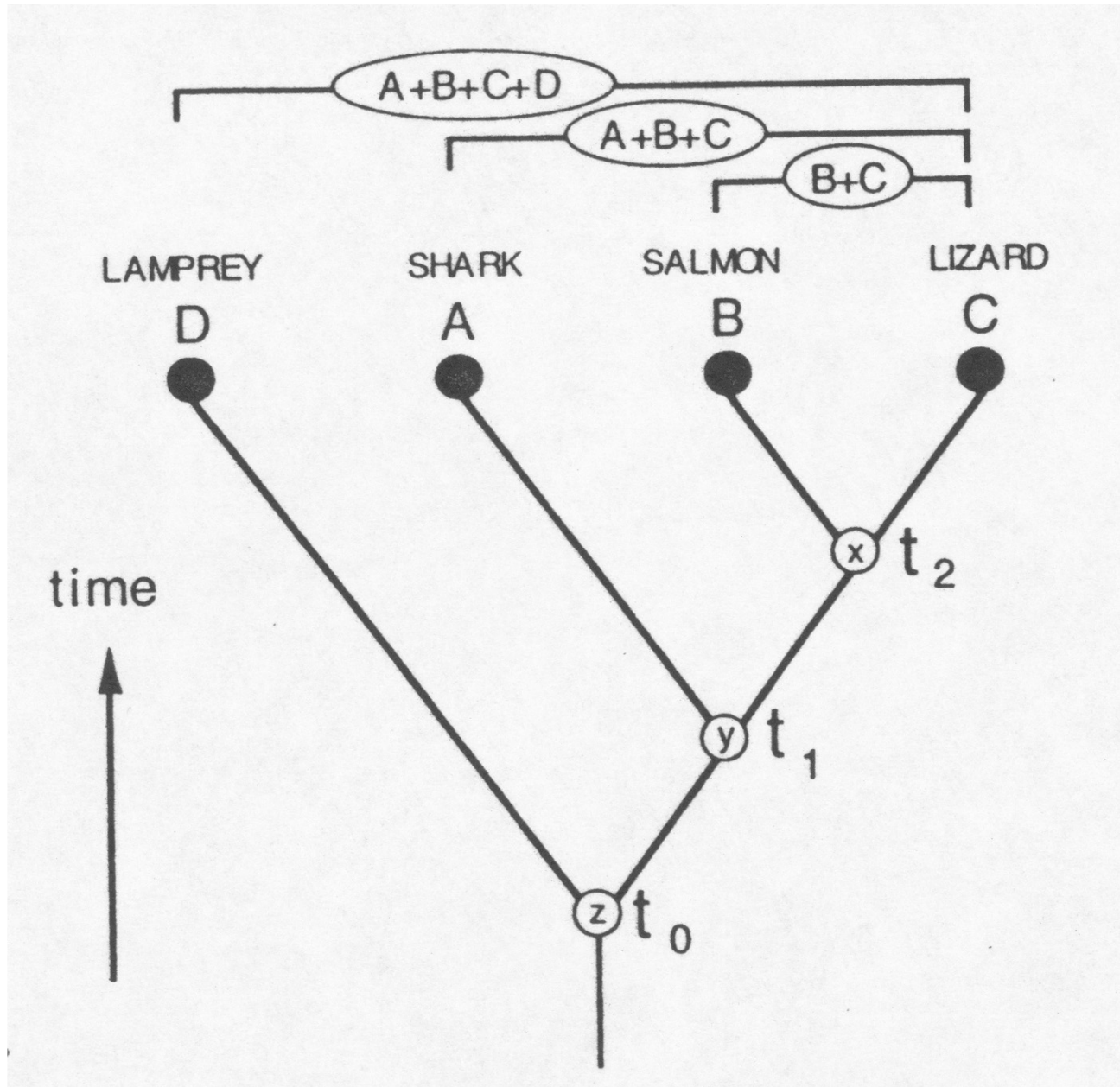
Apomorfia

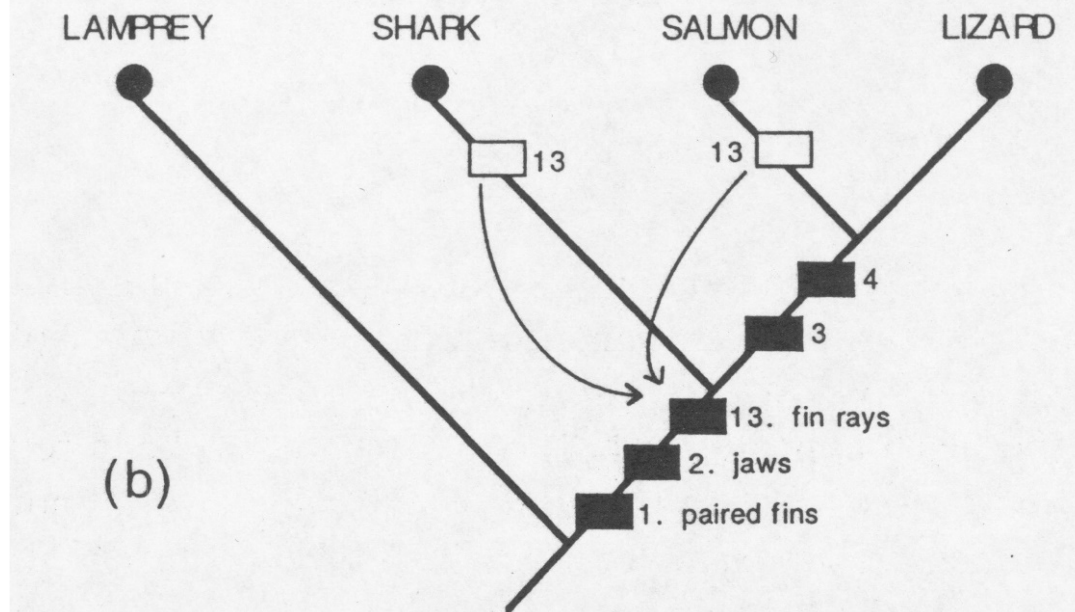
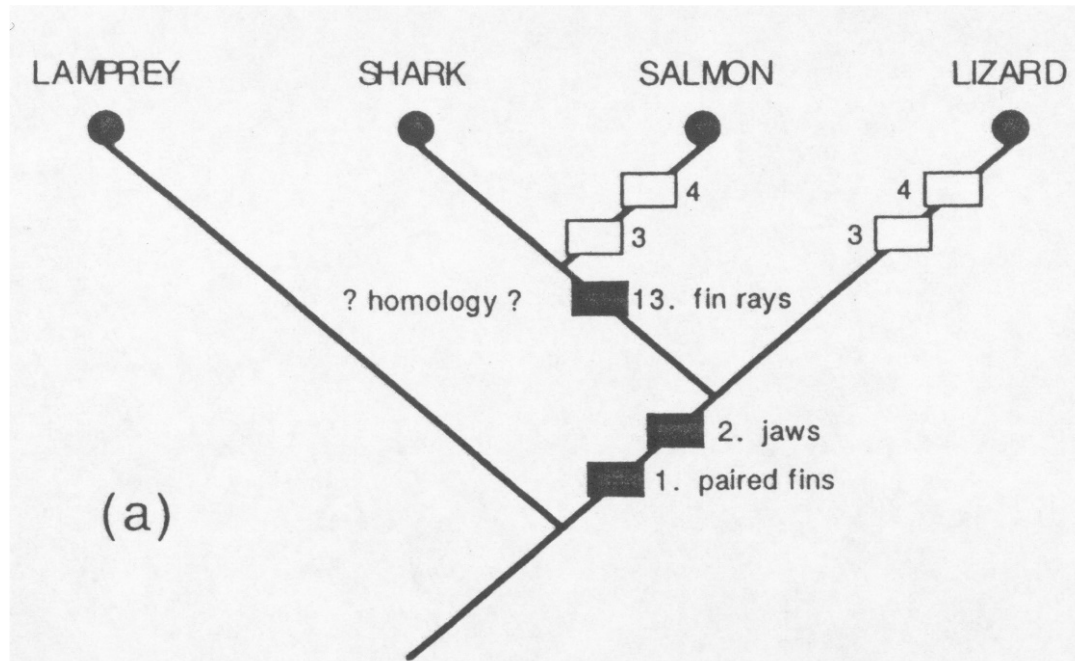
Autapomorfia

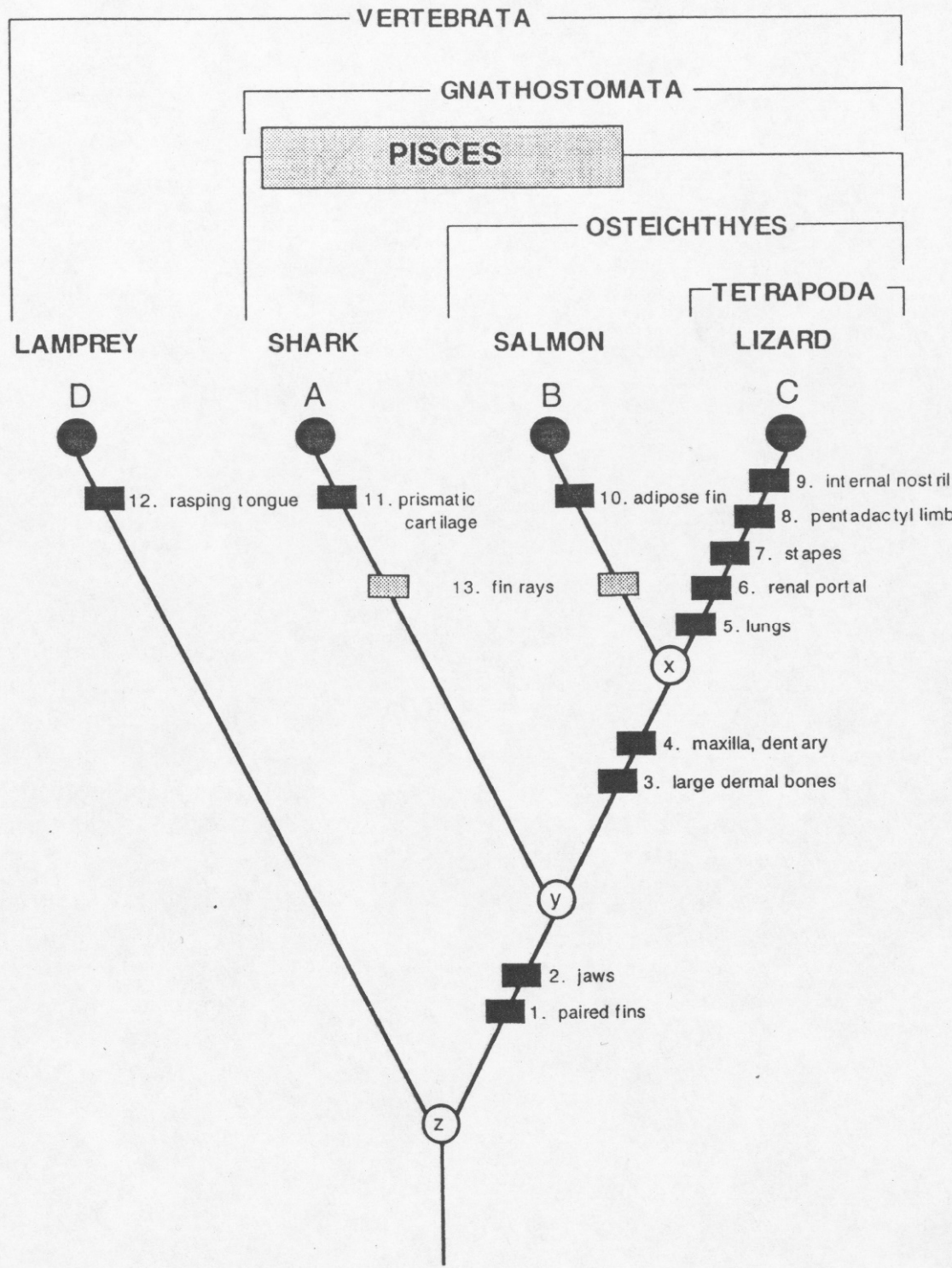
Synapomorfia

**Homoplázia** = konvergencia + paralelizmus

**Mimoskupinové porovnanie** (outgroup comparison)







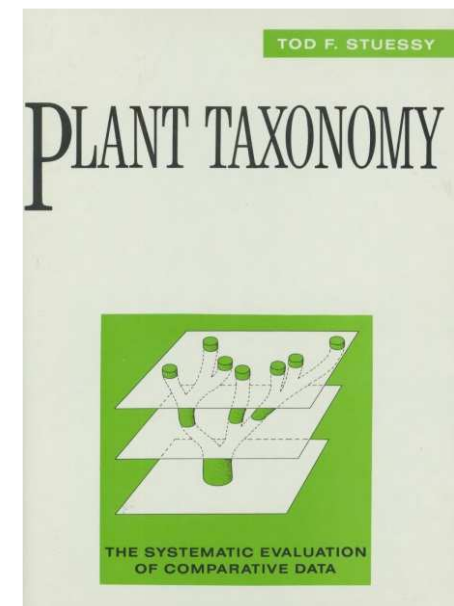
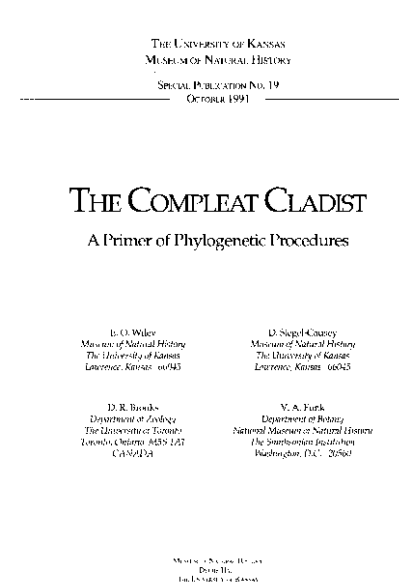
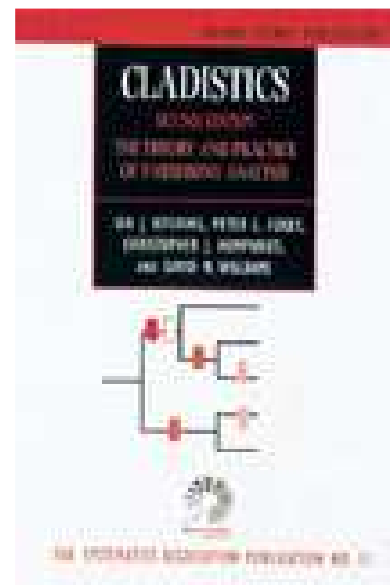
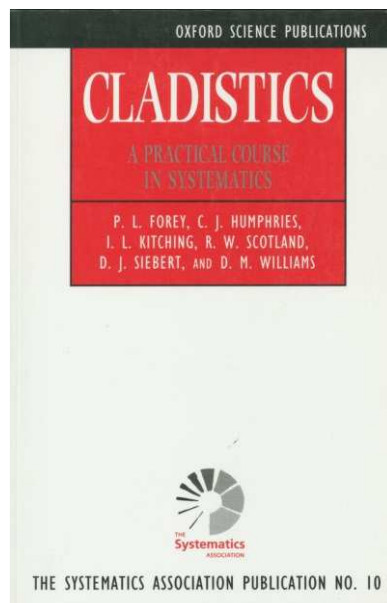
Forey, P.L., Humphries, C.J., Kitching, I.J., Scotland, R.W., Siebert, D.J. & Williams, D.M., 1992. *Cladistics. A practical course in systematics*. Clarendon Press, Oxford.

Kitching, I.J., Forey, P.L., Humphries, C.J. & Williams, D.M., 1998. *Cladistics. The theory and practice of parsimony analysis*. Ed. 2. Oxford University Press, Oxford.

Stuessy, T. F. 1990. *Plant taxonomy: the systematic evaluation of comparative data*. Columbia University Press, New York.

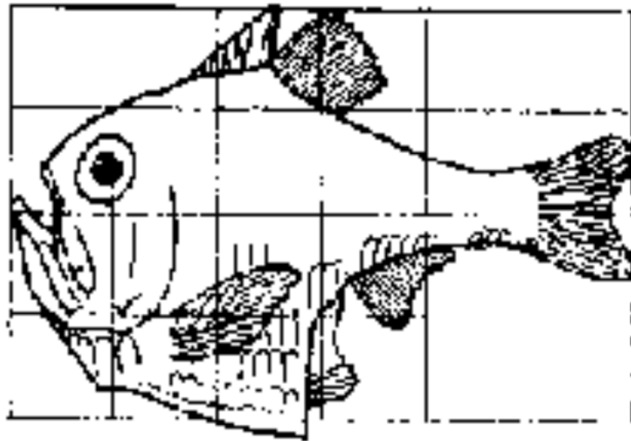
Wiley, E.O., Siegel-Causey, D., Brooks, D.R. & Funk, V.A. 1991. *The compleat cladist, a primer of phylogenetic procedures*. The University of Kansas, Museum of Natural History, Lawrence.

K dispozícii na www stránke: <http://nhm.ku.edu/cc.html>

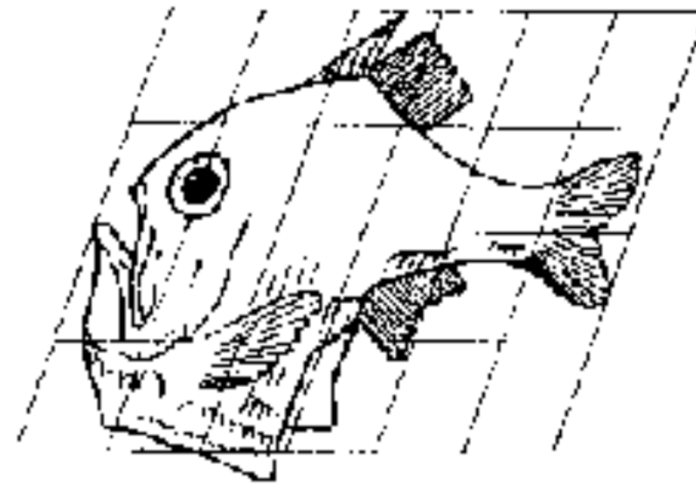


## Geometrická morfometrika

**Thompson, A. W. 1917.** *On growth and form.* Cambridge University Press, Cambridge.

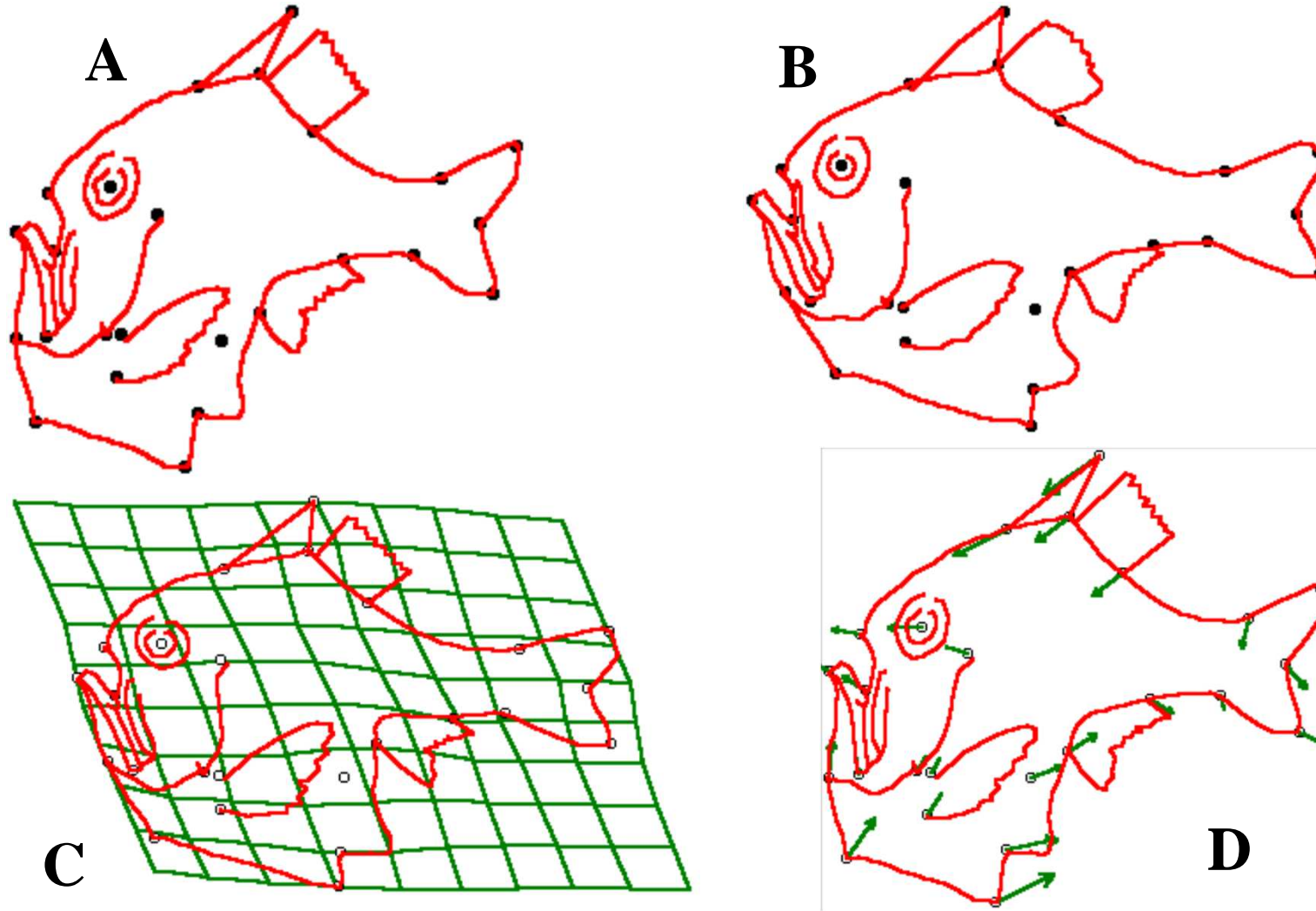


*Argyropelecus olfersi.*



*Sternoptyx diaphana.*

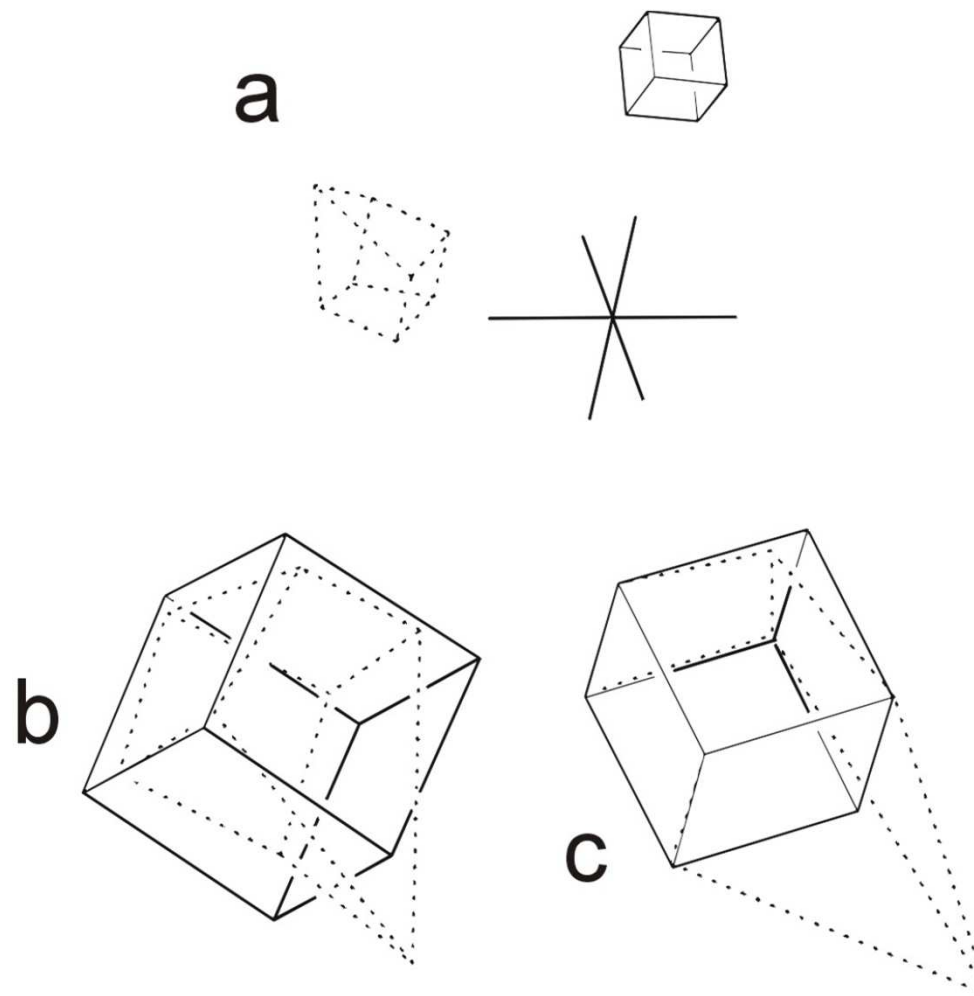
# Geometrická morfometrika



Vzájomné vzťahy tvarov druhov *Stenoptyx diaphana* (A) a *Argyropelecus olfersi* (B) – vzorové dáta z programu tpsSpline (<http://life.bio.sunysb.edu/morph/>), C – zobrazenie celkovej transformácie pomocou ohybnej pásky (*thin-plate spline*), D – to isté vyjadrené pomocou vektorov



# Geometrická morfometrika



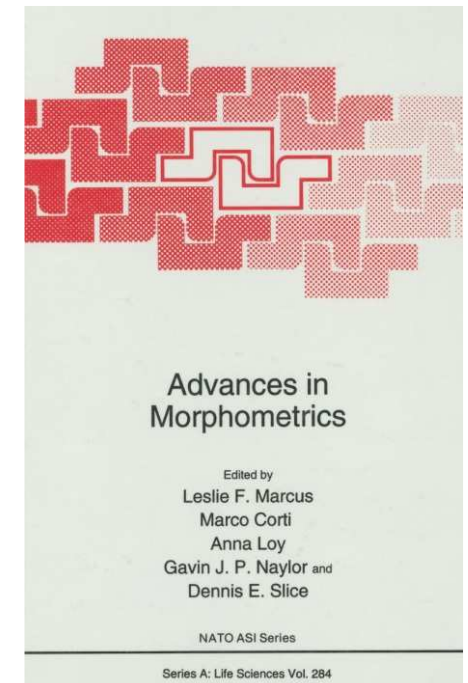
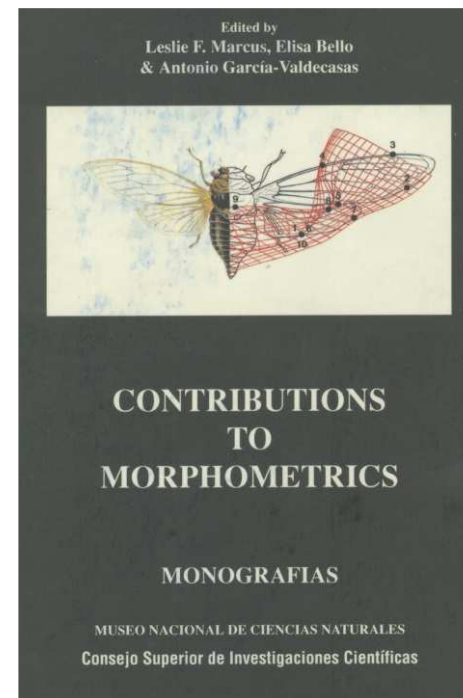
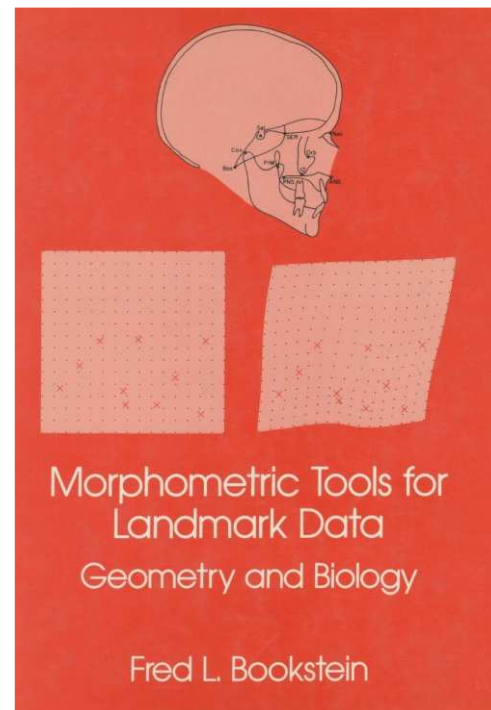
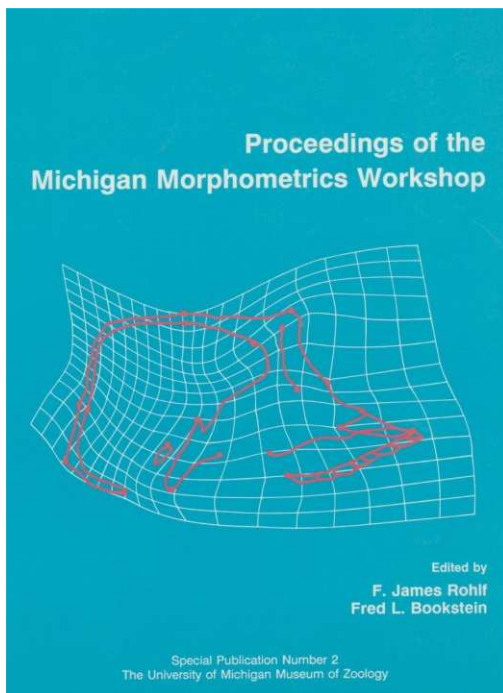
**Prokrustova analýza.** a – konsenzuálna konfigurácia plnou čiarou, jednotlivý objekt bodkovane; b – superpozícia metódou GLS (rozdíely v pozícii zodpovedajúcich význačných bodov sú porovnateľné); c – superpozícia metódou rezistentného prispôsobenia (objekty sa výrazne líšia v pozícii jediného bodu)

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