Hennigs method
characters (transformation series)

| outgroup | 0 | 0 | 0 | 0 | 0 |
| ---: | :--- | :--- | :--- | :--- | :--- |
| A | 1 | 0 | 0 | 0 | 1 |
| B | 1 | 1 | 0 | 1 | 0 |
| C | 1 | 0 | 1 | 1 | 0 |




## Wagner algorithm

First we have to introduce few terms (or definitions):

1) A particular character ( X ) of a particular taxon (A) is defined as $\mathrm{X}(\mathrm{A}, i)$, where $i$ is the $i$ th character in a vector of $i$ characters.
2) The vector of characters for a particular taxon is defined as $\Sigma \mathrm{X}(\mathrm{A}, \mathrm{i})$. For example, the character vector for M is:

$$
\Sigma \mathrm{X}(\mathrm{~A}, i)=110000 .
$$

3) The difference (D) between two taxa is the sum of the absolute differences between their characters:

$$
\mathrm{D}(\mathrm{C}, \mathrm{~B})=\Sigma|\mathrm{X}(\mathrm{C}, i)-\mathrm{X}(\mathrm{~B}, i)| .
$$

We calculate this in the following manner :

$$
\begin{gathered}
\mathrm{D}(\mathrm{C}, \mathrm{~B})=\Sigma|\mathrm{X}(\mathrm{C}, \mathrm{i})-\mathrm{X}(\mathrm{~B}, i)|= \\
=(1-1)+(0-0)+(1-1)+(1-0)+(0-1)+(1-0)=3
\end{gathered}
$$

Taxon

| ANC | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | 1 | 1 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 1 | 0 | 1 | 0 |
| C | 1 | 0 | 1 | 1 | 0 | 1 |

4) The interval (INT) of a taxon is the length of the line between that taxon and its ancestor. For example, the interval of B is:
$\operatorname{INT}(\mathrm{B})=\mathrm{D}[\mathrm{B}, \mathrm{ANC}(\mathrm{B})]$
where $\operatorname{INT}(B)$ is the interval of taxon $B, A N C(B)$ is the hypothetical ancestor of B , and $\mathrm{D}[\mathrm{B}, \mathrm{ANC}(\mathrm{B})]$ is the path length distance of B to its ancestor.

| ANC | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | 1 | 1 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 1 | 0 | 1 | 0 |
| C | 1 | 0 | 1 | 1 | 0 | 1 |

1. ANC vector in table represents the outgroup.
2. We calculate difference D from ANC for each taxon:
$\mathrm{D}(\mathrm{A}, \mathrm{ANC})=2$
$D(B, A N C)=3$
$\mathrm{D}(\mathrm{C}, \mathrm{ANC})=4$.
3. We create interval for this taxon. A is closest (in difference) to ANC, so we will build the interval INT(A,ANC):
$\operatorname{INT}(\mathrm{A}, \mathrm{ANC})=\mathrm{D}(\mathrm{A}, \mathrm{ANC})=2$.
4. We select taxon, that has smallest difference D to ANC. It is taxon B. 5. Then we will look for the interval, that has smallest difference $D$ to the taxon B. Currently there is only one interval INT(A,ANC), so there is no choice. So we do not need to calculate $\mathrm{D}[\mathrm{B}, \mathrm{INT}(\mathrm{A})]$.
5. We connect B to INT(A), by constructing hypothetical ancestor (X), characters of which are medians of transformation series ANC, A and B, so those three taxa that we included until now.

| Taxon | Characters |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| ANC | 0 | 0 | 0 | 0 | 0 | 0 |
| A | 1 | 1 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 1 | 0 | 1 | 0 |
| X (median) | 1 | 0 | 0 | 0 | 0 | 0 |


| ANC | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | 1 | 1 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 1 | 0 | 1 | 0 |
| X (median) | 1 | 0 | 0 | 0 | 0 | 0 |


7. Going back to the step 4 of algorithm, we add further taxon, which has smallest D to ANC. There is only one remaining taxon, C. According to algorithm we should connect it with the interval that has smallest difference to C. Therefore, we must calculate three interval difference values, one for each interval in the tree. For this we have to calculate differences between taxa, their ancestors and taxon C (we already know the difference between C and ANC):

$$
\begin{aligned}
& \mathrm{D}(\mathrm{~A}, \mathrm{X})=|\mathrm{X}(\mathrm{~A}, i)-\mathrm{X}(\mathrm{X}, i)|=1 \\
& \mathrm{D}(\mathrm{~B}, \mathrm{X})=|\mathrm{X}(\mathrm{~B}, i)-\mathrm{X}(\mathrm{X}, i)|=2 \\
& \mathrm{D}(\mathrm{C}, \mathrm{X})=|\mathrm{X}(\mathrm{C}, \mathrm{i})-\mathrm{X}(\mathrm{X}, i)|=3 \\
& \mathrm{D}(\mathrm{C}, \mathrm{~A})=|\mathrm{X}(\mathrm{C}, i)-\mathrm{X}(\mathrm{~A}, i)|=4 \\
& \mathrm{D}(\mathrm{C}, \mathrm{~B})=|\mathrm{X}(\mathrm{C}, i)-\mathrm{X}(\mathrm{~B}, i)|=3 \\
& \mathrm{D}(\mathrm{X}, \mathrm{ANC})=|\mathrm{X}(\mathrm{X}, \mathrm{i})-\mathrm{X}(\mathrm{ANC}, i)|=1
\end{aligned}
$$

| ANC | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | 1 | 1 | 0 | 0 | 0 | 0 |
| B | 1 | 0 | 1 | 0 | 1 | 0 |
| X (median) | 1 | 0 | 0 | 0 | 0 | 0 |

So we can calculate differences to intervals:
$\mathrm{D}[\mathrm{C}, \mathrm{INT}(\mathrm{A})]=\mathrm{D}(\mathrm{C}, \mathrm{A})+\mathrm{D}(\mathrm{C}, \mathrm{X})-\mathrm{D}(\mathrm{A}, \mathrm{X}) / 2=(4+3-1) / 2=3$
$\mathrm{D}[\mathrm{C}, \mathrm{INT}(\mathrm{B})]=\mathrm{D}(\mathrm{C}, \mathrm{B})+\mathrm{D}(\mathrm{C}, \mathrm{X})-\mathrm{D}(\mathrm{B}, \mathrm{X}) / 2=(3+3-2) / 2=2$
$\mathrm{D}[\mathrm{C}, \mathrm{INT}(\mathrm{X})]=\mathrm{D}(\mathrm{C}, \mathrm{X})+\mathrm{D}(\mathrm{C}, \mathrm{ANC})-\mathrm{D}(\mathrm{X}, \mathrm{ANC}) / 2=(3+4-1) / 2=3$
Because the difference between C and $\operatorname{INT}(\mathrm{B})$ has the smallest value, we construct another hypothetical ancestor $(\mathrm{Y})$ and connect C to the tree through this new ancestor to $\operatorname{INT}(\mathrm{B})$. To calculate the character vector for this new ancestor, take the median of the vectors of the three appropriate taxa, X, B, and C. So we have the resulting tree:



Taxon
Characters

| X | 1 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| B | 1 | 0 | 1 | 0 | 1 | 0 |
| C | 1 | 0 | 1 | 1 | 0 | 1 |
| Y (median) | 1 | 0 | 1 | 0 | 0 | 0 |

## Phylogenetic tree building methods

## method of building

 treesclustering algorithm
optimality criterion
type of data
DNA sequences or other characters

UPGMA
neighbor-joining tree
minimum
evolution
tree
parsimony
maximum likelihood
Bayesian analysis

Willi Hennig (German edition 1950, Spanish edition 1965, English edition 1966, 1968)

Evolutionary relationships are inferred from SYNAPOMORPHIES descendant states, similarity - based on common origin (HOMOLOGY)
Hennig did not provide any method for identification of synapomorphies.

Farris (1967, 1970, 1972, 1973, 1976, 1977, 1979, 1980, 1982, et al. 1970, and others)

Criterion for identification of synapomophies is PARSIMONY

## Maximum parsimony (MP)

Simple, intuitive and logical method (based on Medieval logic,
Occam's razor - prefers the simplest solutions), no statistics
Minimalizes ad hoc explanations - homoplasy
Maximizes explanatory value


## Parsimony can provide misleading results - long branch attraction

Felsenstein zone - some branches or internodes look shorter because of numerous mutations
A -> C -> A, etc.


## Parsimony

1) Wagner parsimony: treats characters as ordered such that the change from one character to another implies change through any intervening characters in the transformation series. Characters are allowed to reverse freely.
2) Fitch parsimony: treats characters in a transformation series as unordered such that change from one character to another character within a transformation series does not imply changes through possible intervening characters. Characters are allowed to reverse freely.
3) Dollo parsimony: requires every synapomorphy to be uniquely derived, i.e., appearing only once on the tree. The synapomorphy may reverse, but once reversed it cannot reappear. But a "relaxed" Dollo criterion, which amounts to assigning a weight to the cost of reversal, might be more appropriate in some cases.
4) Camin-Sokal parsimony: makes the assumption that character evolution is irreversible. This is true, philosophically, because time is irreversible and the reversals are really new apormorphies. But we cannot know this a priori. This criterion is rarely used.

Simple parsimony: selection of the optimal cladogram depends only on the amount of the character changes on the tree, reversals and parallelisms have an equal value.

General parsimony: depends on more detailed knowledge of characters. Some characters might be treated as ordered, others as unerdered, in some cases certain characters might have higher weight.

Equally parsimonious trees:

1. equal topology, but different interpretation of characters - phylogenetic relationships are identical, resulting classification is the same.
2. different topology - phylogenetic relationships are different, resulting classifications are different

Consistency index, CI, Kluge a Farris (1969) measures of how transformation series and entire data matrices "fit" particular tree topologies. The consistency index is the ratio of the minimum amount of changes (steps) it might show in the matrix ( $\mathbf{m}$ ) and the amount of change (steps) it does show on a particular tree (s) multiplied by 100: $\quad \mathrm{CI}=\mathrm{m} / \mathrm{s} \times 100$



Summary of the character changes in the cladogram:

Transf. series
1
2
3
4
5
6
changes
0 -> 1
$0->1$
0 -> 1
$0->1$
$0->1$
0 -> 1 -> 0

Total amount of changes (steps) in the cladogram is 7 then $C I=6 / 7 \times 100=85,7$

Retention index, RI, Farris (1989) The retention index measures the fraction of apparent synapomorphy to actual synapomorphy:
$R I=(g-s) /(g-m) \times 100$
$\mathrm{s}, \mathrm{m}$ defined the same way as for CI, g how many steps would it take to explain evolution within the transformation series under the worst possible condition, which is totoal amount of taxa with character 1 or 0 (whichever is smaller), summarized for all transformation series (resp. characters).

|  |  | transformation series |  |  | 5 | 6 | transf. series changes |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |  |  | 1 | 0 -> 1 |
|  |  |  |  |  |  |  | 2 | $0->1$ |
| OG | 0 | 0 | 0 | 0 | 0 | 0 | 3 | $0->1$ |
| taxon A | 1 | 0 | 0 | 0 | 0 | 1 | 4 | $0->1$ |
| B | 1 | 1 | 0 | 0 | 0 | 1 | 5 | $0->1$ |
| C | 1 | 1 | 1 | 0 | 0 | 1 | 6 | 0 -> 1 |
| D | 1 | 1 | 1 | 1 | 0 | 1 |  |  |
| E | 1 | 1 | 1 | 1 | 1 | 0 | Total | changes of |
| F | 1 | 1 | 1 | 1 | 1 | 0 | charac | matrix is 6 . |



Summary of the character changes in the cladogram:

Transf. series
1
2
3
4
5
6
changes
0 -> 1
$0->1$
$0->1$
$0->1$
$0->1$
0 -> 1 -> 0

CI index is equal, even if cladogram is different

Total amount of changes (steps) in the cladogram is 7 then $\quad \mathrm{CI}=6 / 7 \times 100=85,7$


Total maximum amount of steps is 13


Optimizing trees
a posteriori activity that does not help to construct trees but evaluates already constructed trees. In the case that we have more equally parsimonious trees of the same topology, taking into account the some features of characters we may select tree where we prefer parallelisms or reversals.


# DELTRAN <br> DELays evolutionary <br> TRANSformation of a character on a tree 

reversals

ACCTRAN

ACCelerates evolutionary
TRANsformation of a character on a tree

Tree building methods
Exact methods

Exhaustive search, implicit enumeration Branch-and-bound

Heuristic algorithms
Quick-and-dirty methods, that do not grant that the shortest tree will be found

Improvement of the initial trees

Branch swapping

## Tree building methods

Exhaustive search, implicit enumeration




C2.1














Exhaustive search makes sense up to ca. 11 taxa


## Each unrooted tree (theoretically) can be rooted anywhere along any of its branches



exceeds the number of particles in the known universe!!!

## Tree building methods

Branch-and-bound
Heuristic method is used to find a suboptimal tree, which serves as the first step (starting tree) for the analyses

Uo to ca 25 taxa


## Heuristic algorithms

Quick-and-dirty methods, that do not grant that the shortest tree will be found
Search for
the global
minimum

## Stepwise addition



Branch swapping

## Heuristic algorithms

Stepwise addition
First, three taxa joined


Next, one of the unplaced taxa selected for next addition and placed along one of $\mathbf{3}$ branches.


Each tree is evaluated by the optimality criterion and the best is retained for next round of addition.

Process continues until all objects are put on the tree

Heuristic search is repeated number of times, always with different imnitial three taxa - repeated replications (Nreps in PAUP)

Heuristic algorithm may start also with the Wagner tree, on which we apply branch swaping, while in each step we keep several trees that are further swaped.

## Branch swapping



Nearest neighbor interchange (NNI)





Nearest neighbor interchange (NNI)

## Branch swapping



Subtree pruning and regrafting (SPR)


Subtree pruning and regrafting (SPR)

## Branch swapping




Tree bisection and reconnection (TBR)



Tree bisection and reconnection (TBR)

TBR explores more trees than SPR
TBR is more effective in searching for a short three, but search takes more time

TBR is not the most effective method if we swap the tree, which is rather far from the shortest one - potentially each SPR swap is able to find short tree in such case

## Consensus trees



Majority-rule


Strict consensus trees


## Majority-rule

## Trees:



How many times each partition of species is found:

AE|BCDF 3
ACE|BDF
ACEF|BD AC | BDEF AEF|BCD 1 ADEF|BC 2
ABDF|EC 1
ABCE|DF 3
3111

Majority-rule consensus tree of the unrooted trees:


## Strict consensus

 trees

## Strict consensus trees


components

Uncertain position of a single individual may cause colaps of the tree (even strong signal in data can be overturn by one problematic individual)


## Components

Polytomy is a consequence of:

1. Insufficient data - we do not have enough variation to get reliable tree
2. Conflict in data - characters equally support position of the taxon on more than one place on the tree ( => missing data)

Polytomy should not be interpreted as rapid radiation there is an uncertainty in the data!!!

## Adams consensus trees



Taxa causing conflicts are moved to the node, where they do not cause conflict with any tree





Adams consensus tree

## Bootstrap

- Uses random sampling with replacement (we create replicated data matrices)
- We analyze each replicated data set
- Looking for the same branches that appear on the tree
original data matrix replicated data matrix

```
*
```

| taxóny | znaky |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 2 | 5 | 5 | 6 | 6 | 8 |
| A | R | R | R | Y | Y | Y | Y | Y |
| B | R | R | R | Y | Y | Y | Y | Y |
| C | Y | Y | Y | Y | Y | R | R | R |
| D | Y | Y | Y | R | R | R | R | R |
| Outgp | R | R | R | R | R | R | R | R |

## Bootstrap



## Jack-knife

- Jack-knife is similar to the bootstrap, it differs only in the strategy of selection of characters
- Randomly selected characters are deleted from the matrix (e.g., 50\%)
- Jack-knife seldom occurs in statistical packages and is also seldom used
- Jack-knife and bootstrap have tendency to produce similar results


## Bremer support = decay analysis

Bremer support can be expressed as a number of further steps on the tree that result in the collapse of the branch into polytomy in the strict consensus tree.

Branches on the tree that collapse during the building of the strict consensus tree from all most parsimonious (shortest) trees possess value of the Bremmer support $=0$, such support is usually not presented (neither branched with such support).

When we add to all most parsimonious (shortest) trees all trees that are one step longer, some branches will collapse, they possess value of Bremmer support = 1, etc.

## Bremer support = decay analysis

There are two possible strategies of the calculation of the Bremer support:
(1) Calculate all cladograms that are certain amount of steps longer than most parsimonious trees and search at which length of the tree given branch collapses (disappears).
(2) Calculate all possible trees that do not contain given branch and measure their length (metóda „reverse constraints")

ATTENTION: computing of the Bremer support is time consuming, if interrupted earlier acquired values of Bremer support are too high


## Rules of Phylogenetic Classifications

1. Only monophyletic groups will be formally classified
2. All classifications will be logically consistent with the phylogenetic hypothesis accepted by the investigator
3. Regardless of the conventions used, each classification must be capable of expressing the sister group relationships among the taxa classified

## Conventions

1. The Linnaean system of ranks will be used
2. Minimum taxonomic decisions will be made to construct a classification or to modify existing classifications.
3. Taxa forming an asymmetrical part of a phylogenetic tree may be placed at the same rank and sequenced in their order of branching; When such a list is encountered, the sequence of the list denotes the sequence of the branching.

Subphyllum Vertebrata
Infraphyllum Myxinioidea Infraphyllum Petromyzontia Infraphyllum Gnathostomata

4. Taxa whose relationships are polytomous will be placed sedis mutabilis at the same rank


Subphyllum Vertebrata<br>Infraphyllum Myxinioidea (sedis mutabilis) Infraphyllum Petromyzontia (sedis mutabilis) Infraphyllum Gnathostomata (sedis mutabilis) Superclass Chondrichthys Superclass Teleostomi

5. Monophyletic taxa of uncertain relationships will be placed incertae sedis at a level in the hierarchy where their relationships are known with some certainty
6. A group whose qualities are not known may be included in a phylogenetic classification if it is treated as incertae sedis and its name is put in shutter quotes (quotation marks)

7. Fossil taxa will be treated differently than Recent taxa. Fossil taxa will always be sequenced with their Recent relatives following Convention 3. If they are ranked, their status as fossils will be denoted by placing a dagger or cross symbol before the rank (Nelson, 1972). Alternatively, they may be given the neutral rank of "plesion".As natural taxa, monophyletic fossil taxa may stand incertae sedis or sedis mutabilis, just as any Recent natural taxon.
a Infradivision Theria
Supercohort Marsupialia
Supercohort Eutheria
b Infradivision Theria
Plesion Kueneotherium
Plesion Symmetrodonta
Plesion Dryolestoidea
Plesion Paramus
Supercohort Marsupialia
Supercohort Eutheria
c Infradivision Theria
$\dagger$ Supercohort Kueneotheria
$\dagger$ Supercohort Symmetrodontia
$\dagger$ Supercohort Dryolestia
$\dagger$ Supercohort Paramia
Supercohort Marsupialia
Supercohort Eutheria
8. Stem species (ancestral species) are placed in classifications in parentheses beside the names of taxa they gave rise to or taxa containing their descendants, as appropriate.


## Cladistic biogeography



