

Multivariate methods in taxonomy

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Presentations available at:

<https://botany.natur.cuni.cz/brassiploidy>

Phenetic approach (multivariate methods; “pattern”; cluster analysis, ordination methods, discriminant analysis)

Cladistic approach (parsimony analysis)

Alternative approaches to the phylogenetic reconstruction (neighbour joining method, maximum likelihood, Bayesian statistical methods)

Geometric morfometrics (Booksteinove shape coordinates, Procrustes analysis, thin plate spline method)

Software: MorphoTools2, SYN-TAX 2000

Phenetic approach

Michel Adanson (1727-1806)

Familles des Plantes (1763)

65 different classifications, each based on one character (e.g. placentation, type of inflorescence ...)

P R E F A C E			
11. Blitons.	12. Q. Pourpier.	10. Orchis.	21. P. Chevre-feuille.
17. CLASSE.	41. Q. Rosera.	11. Aristoloches.	22. M. Aireles.
<i>Etamines sur le Calice & sur l'Overe ensemble.</i>	18. CLASSE.	20. CLASSE.	23. Apocins.
	<i>Etamines sur l'Overe.</i>	<i>Etamines sur la Corole.</i>	24. Borraghes.
12. Elagues.	9. 6. Jousabres.	9. 10. Jousabres.	25. Labites.
13. Onagres.	11. 11. Aristoloches.	16. Composées.	26. Vervènes.
14. Mirtes.	19. CLASSE.	17. Campanules.	27. Personées.
15. Umbellifères.	<i>Etamines sur le fil de l'Overe.</i>	18. Bionces.	28. Solanons.
16. 2. Chevre-feuille.		19. Apocins.	29. Anagallis.
		20. Scabieuses.	31. Q. Pourpier.
			32. Q. Jousbarbes.
			34. Q. Alines.
	42. Système. Etamines; leur figure respective.		
1. CLASSE.	11. Chevre-feuilles.	3. CLASSE.	5. CLASSE.
<i>Plantes sans Etamines.</i>	12. Aireles.	<i>Etamines réunies toutes ensemble par les filets en un faisceau.</i>	<i>Etamines réunies par les filets en plus de 2 corps.</i>
1. Bisul.	23. 26. Apocins.	5. 5. Fucus.	41. 2. Légumineux.
2. Champignons.	24. Bourraghes.	6. Palmiers.	52. 2. Crucifères.
3. 6. Fucus.	25. Labites.	8. 2. Liliacés.	54. 7. Cistes.
	26. Vervènes.	11. 4. Aristoloches.	
	27. Personées.	76. Jaiaps.	6. CLASSE.
	28. 9. Solanons.	37. Amarautes.	<i>Etamines réunies par les anteres seulement.</i>
	29. Jalmea.	42. 26. Légumineux.	
	30. Anagallis.	44. 16. Pistachiers.	
	31. Salicées.	45. 21. Timaltes.	
	32. Pourpier.	49. Geraniums.	
	33. Jousbarbes.	50. Mauges.	
	34. Alines.	51. Capriers.	
	35. Blitons.	57. Pins.	
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Phenetic approach

Department of Entomology, University of Kansas, Lawrence, U.S.A.

Michener, Ch.D. & Sokal, R.R. 1957. A quantitative approach to a problem in classification. *Evolution* 11: 130-162.

Department of Microbiology, University of Leicester, U.K.

Sneath, P.H.A. 1957. Some thoughts on bacterial classification. *J. Gen. Microbiol.* 17: 184-200.

Sokal, R.R. & Sneath, P.H.A. 1963. *Principles of numerical taxonomy*. W. H. Freeman and comp., San Francisco & London.

Sneath, P.H.A. & Sokal, R.R. 1973. *Numerical taxonomy, the principles and practice of numerical classification*. W. H. Freeman and comp., San Francisco.

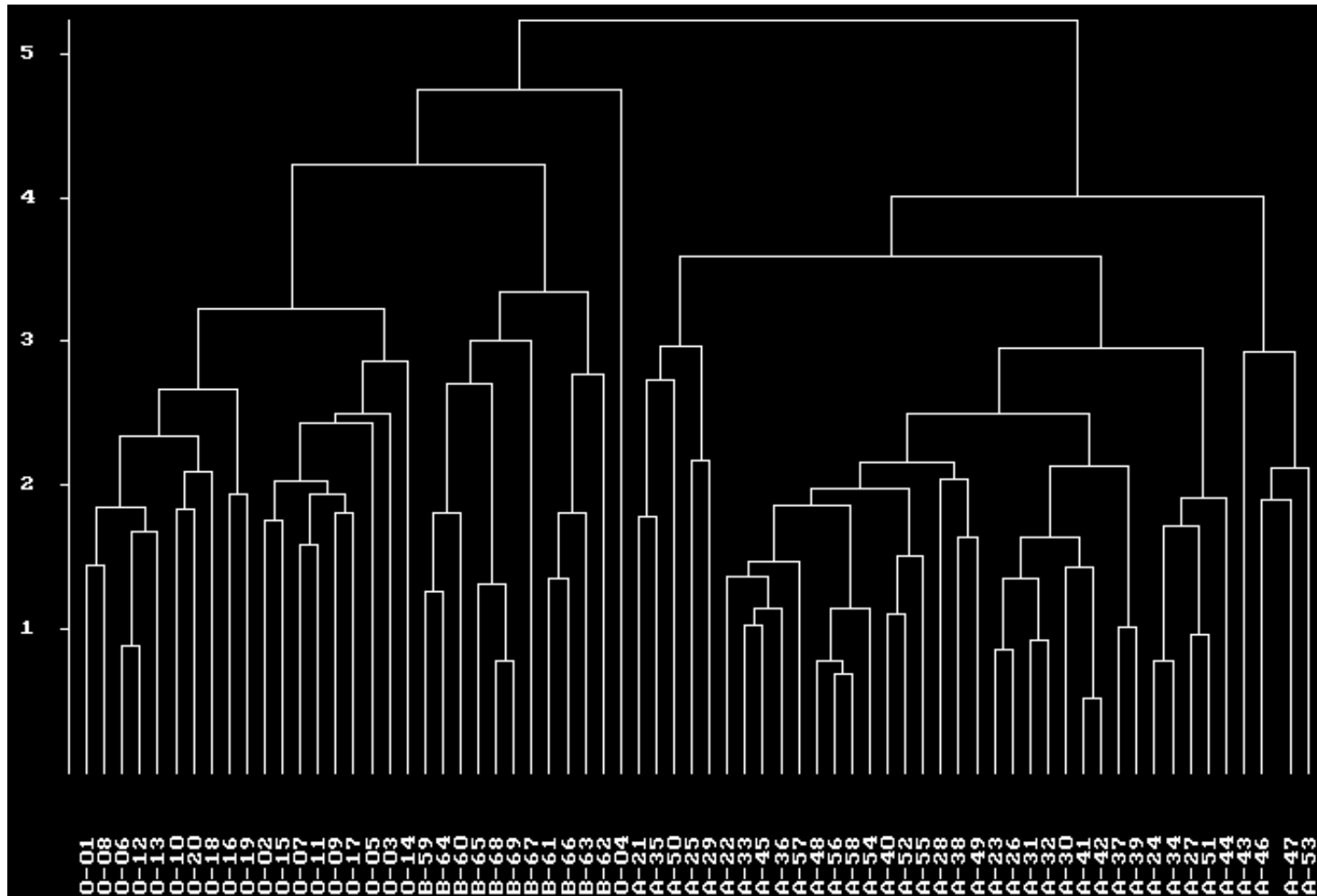
Neo-Adansonian principles

- (1) The ideal taxonomy is that in which the taxa have the greatest content of information and which is based on as many characters as possible.
- (2) A priori, every character is of equal weight in creating natural taxa.
- (3) Overall similarity (or affinity) between any two entities is the function of the similarity of the many characters in which they are being compared.
- (4) Correlation of characters differ in the groups of organisms under study. Thus distinct taxa can be recognized.
- (5) Phylogenetic conclusions can be drawn from the taxonomic structure of a group and from character correlations, assuming some evolutionary mechanisms and pathways.
- (6) The science of taxonomy is viewed and practiced as an empirical science.
- (7) Phenetic similarity is the base of classifications.

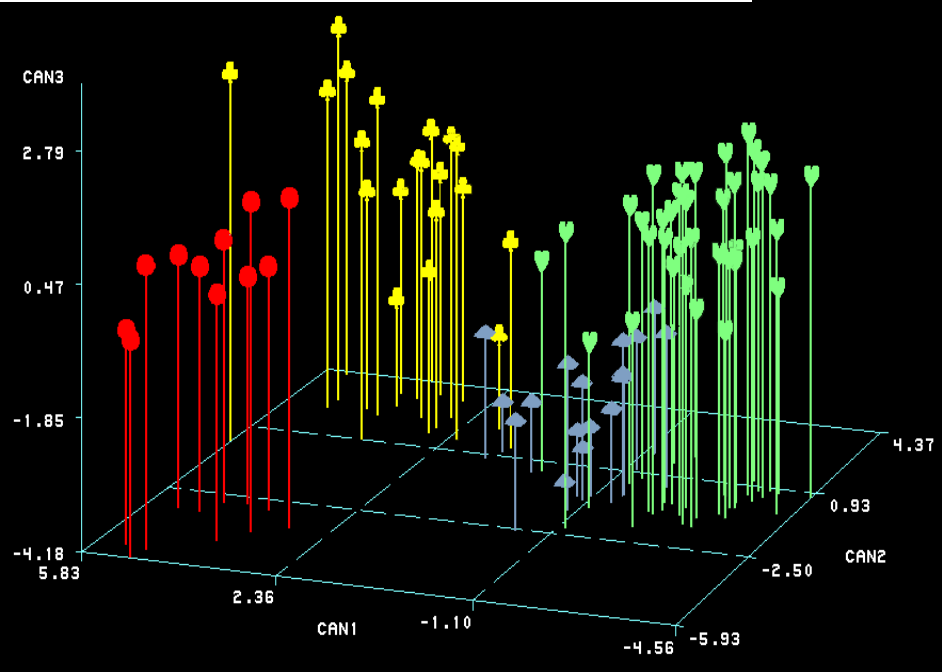
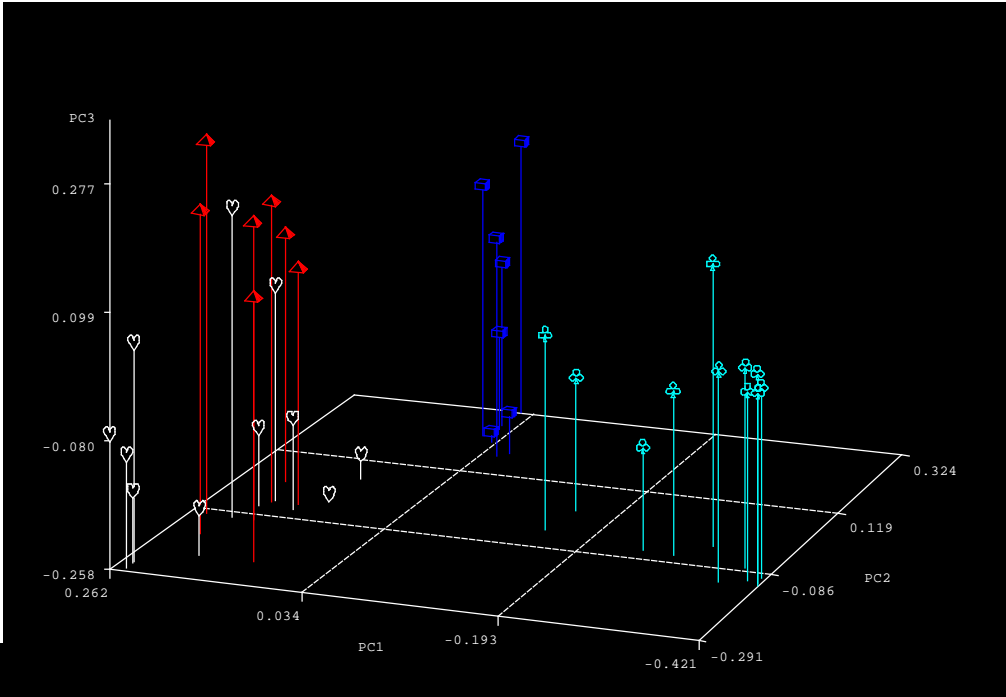
Phenetic approach

- Terms: numerical taxonomy (Sokal & Sneath), statistical systematics (Solbrig), numerical phenetics (Duncan & Baum), multivariate morphometrics (Blackith & Reyment)
- Operational Taxonomic Units (OTU)
- Characters, primary matrix, number of characters, correlations
- Coefficients expressing relationships between characters or objects, secondary matrix
- Multivariate methods (clustering methods, ordination methods, discriminant analysis)
- Different methods may yield different results
- Use of methods in the past and in current taxonomic practice (intraspecific variability, polyploid complexes, study of morphological variability in large areas, molecular data)

Cluster analysis



Principal component analysis



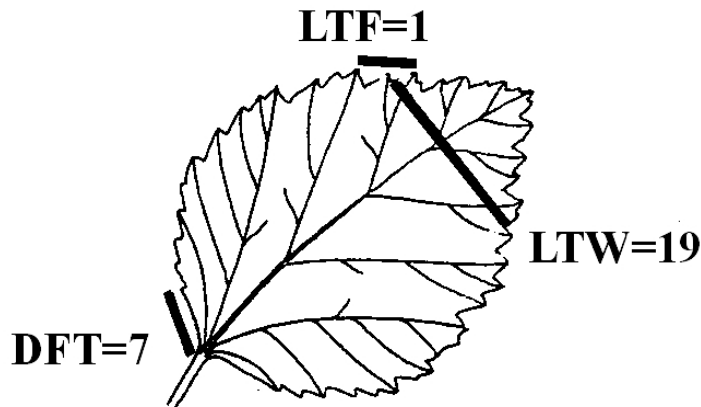
Canonical discriminant analysis

Classificatory discriminant analysis

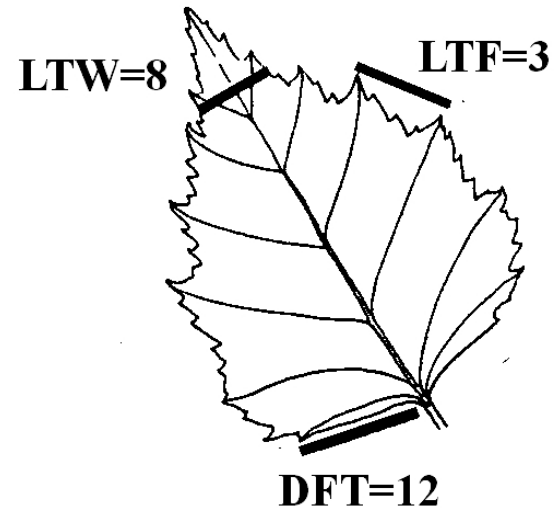
group The affiliation of plants to defined groups predicted based on the established classification criterion (the absolute number and percentage of plants classified into individual groups)

	amara	austr.	olot.	opicii	pyren.	Total
amara	349	20	3	1	7	380
	91.84	5.26	0.79	0.26	1.84	100.00%
austriaca	51	302	1	6	8	368
	13.86	82.07	0.27	1.63	2.17	100.00%
olotensis	2	0	99	0	0	101
	1.98	0.00	98.02	0.00	0.00	100.00%
opicii	1	9	0	326	42	378
	0.26	2.38	0.00	86.24	11.11	100.00%
pyrenaea	1	11	0	19	207	238
	0.42	4.62	0.00	7.98	86.97	

B. pubescens = -35



B. pendula = +21



Discriminant function for determining the species *Betula pubescens* and *B. pendula*:

$$12\text{LTF} + 2\text{DFT} - 2\text{LTW} - 23$$

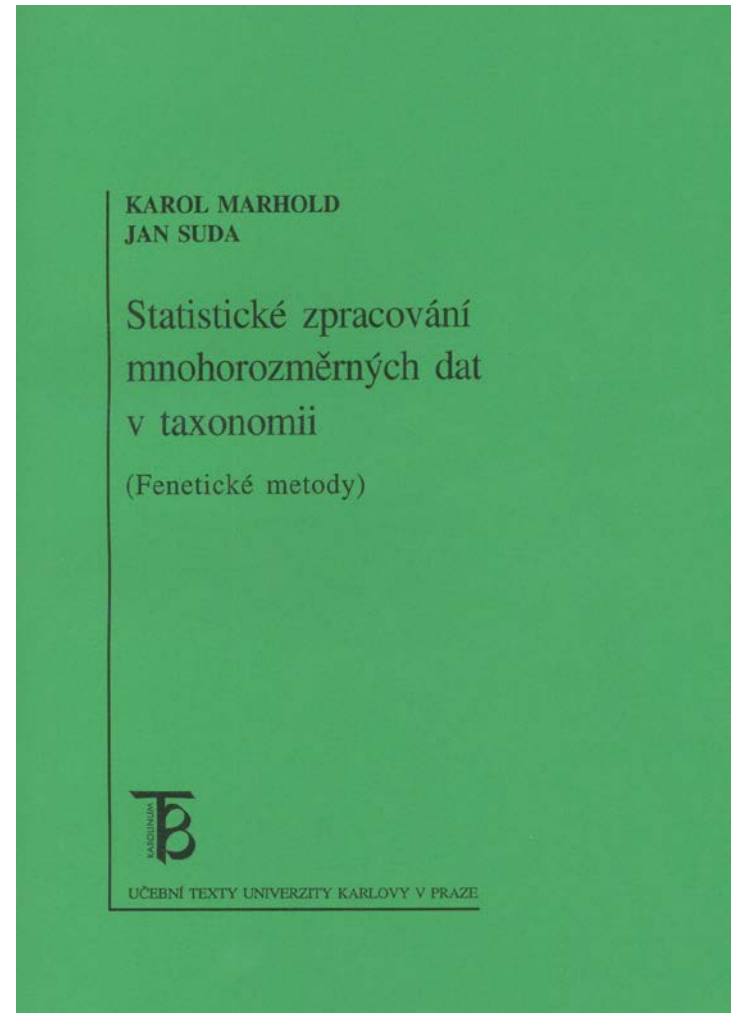
positive values: *B. pendula*

negative values: *B. pubescens*

probability of correct identification: 93%

(Stace, C. A., 1991, *New Flora of the British Isles*)

Marhold, K. & Suda, J. 2002: *Statistické zpracování
mnohorozměrných dat v taxonomii*. Karolinum, Praha.

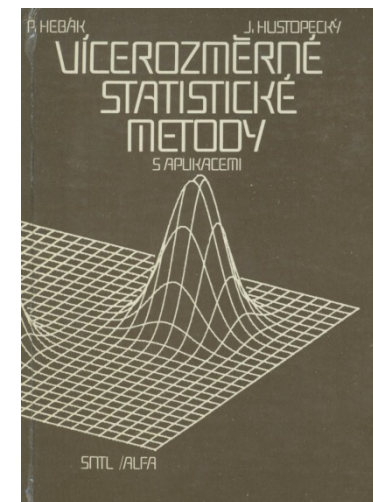


Hebák, P. & Hustopecký, J. 1987: *Vícerozměrné statistické metody s aplikacemi*. SNTL – nakladatelství technické literatury, Alfa, vydavatelství technické a ekonomické literatury, Praha.

Hebák, P., Hustopecký, J., Jarošová, E. & Pecáková, I. 2007. *Vícerozměrné statistické metody (1)*. Ed. 2. Informatorium, Praha.

Hebák, P., Hustopecký, J. & Malá, I. 2005. *Vícerozměrné statistické metody (2)*. Informatorium, Praha.

Hebák, P., Hustopecký, J., Pecáková, I., Průša, M., Řezanková, H., Svobodová, A. & Vlach, P. 2007. *Vícerozměrné statistické metody (3)*. Ed. 2. Informatorium, Praha.

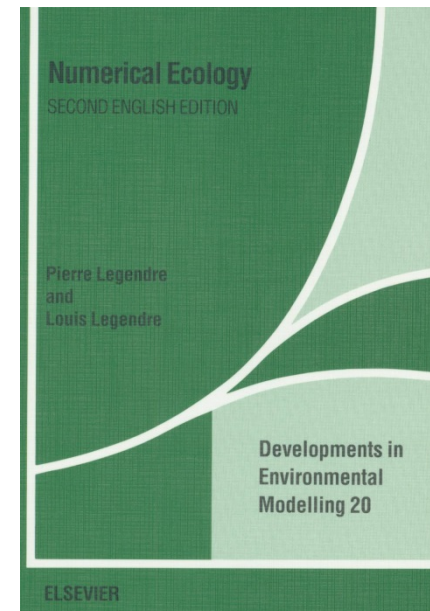
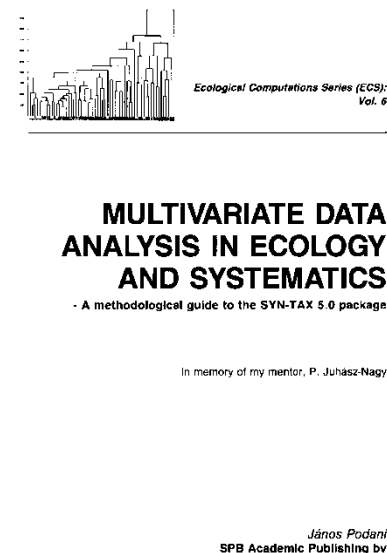
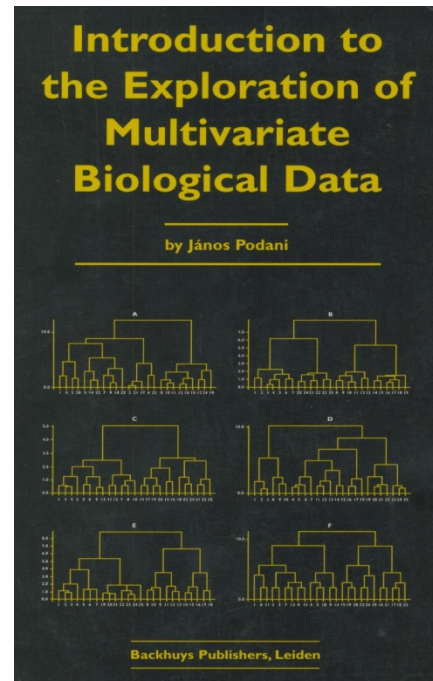
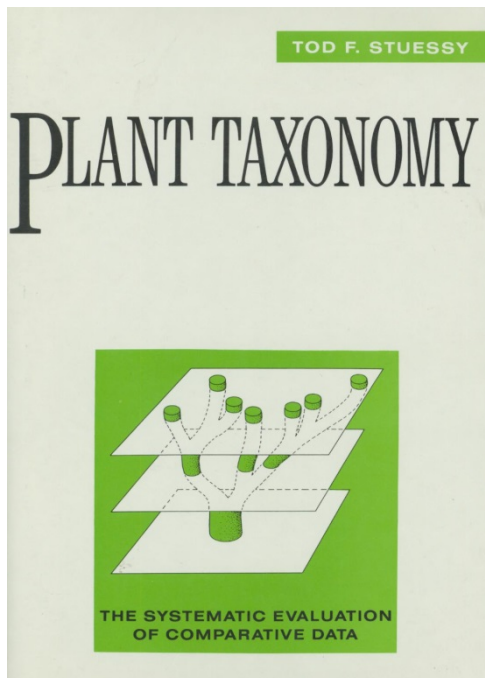


Legendre, P. & Legendre, L. 1998. *Numerical ecology*. Second English edition. Elsevier, Amsterdam.

Podani, J. 1994. *Multivariate data analysis in ecology and systematics*. SPB Academic Publishing bv, The Hague.

Podani, J. 2000. *Introduction to the exploration of multivariate biological data*. Backhuys Publishers, Leiden.

Stuessy, T. F. 1990. *Plant taxonomy: the systematic evaluation of comparative data*. Columbia University Press, New York.



Kladistický přístup

Hennig, W.

1950: *Grundzüge einer Theorie der phylogenetischen Systematik*. Deutsche Zentralverlag, Berlin.

1965: Phylogenetic systematics. *Annual Review of Entomology* 10: 97-116.

1966: *Phylogenetic systematics*. University of Illinois Press, Urbana.

Botany:

Koponen, T., 1968: Generic revision of Mniaceae Mitt. (Bryophyta). *Ann. Bot. Fenn.* 5: 117-151.

Funk, V. & Stuessy, T. F. 1978: Cladistics for practicing plant taxonomist. *Syst. Bot.* 3: 159-178.

Bremer, K. & Wantorp, H.- E. 1978: Phylogenetic systematics in botany. *Taxon* 27: 317-329.

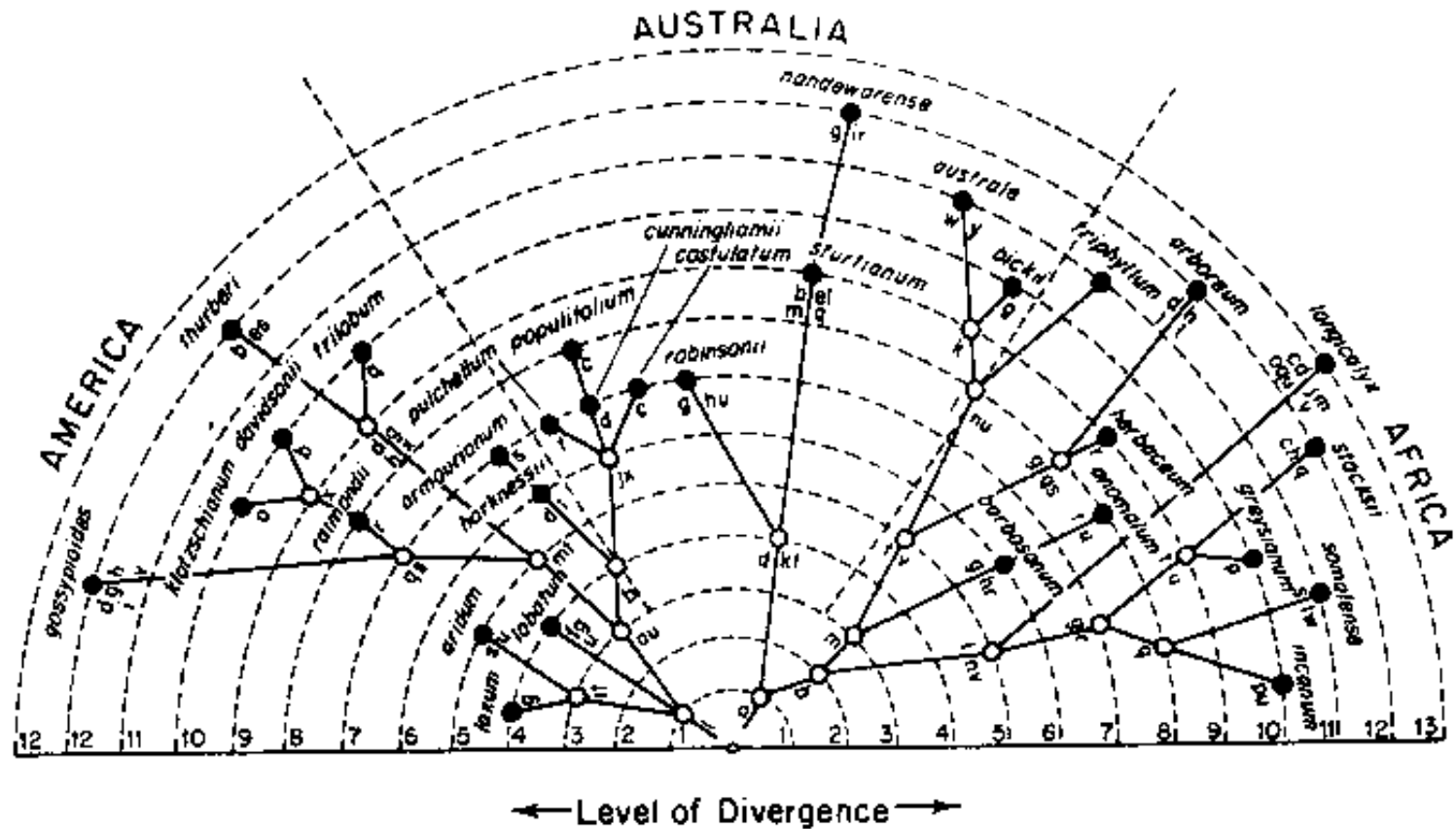


Fig. 2.17 Cladogram (Wagner tree) of 30 species of *Gossypium* (Malvaceae), modified from Frywell¹⁴².

W.H. Wagner, University of Michigan - Groundplan/divergence method

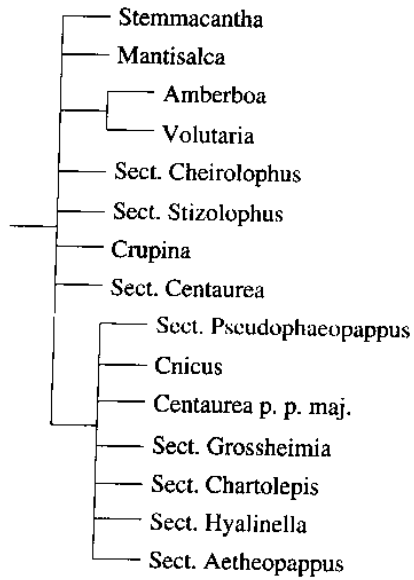


FIGURE 8-4. Strict consensus tree of six equally parsimonious cladograms of *Centaurea* sections and related genera based on cypselas characters from Dittrich (1966, pp. 138-139). The data matrix is given in Table 8-4.

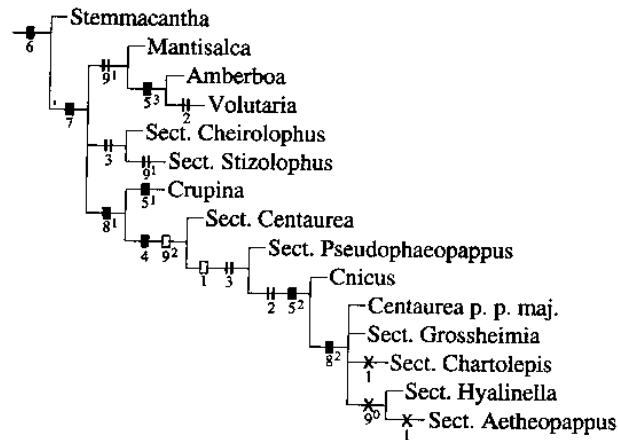


FIGURE 8-5. One of six equally parsimonious cladograms of *Centaurea* sections and related genera based on cypselas characters from Dittrich (1966, pp. 138-139). The characters are given in Table 8-3 and the data matrix in Table 8-4. Solid bars indicate nonhomoplastic synapomorphies; open bars indicate homoplastic synapomorphies with reversals; double bars indicate parallelisms; crosses indicate reversals.

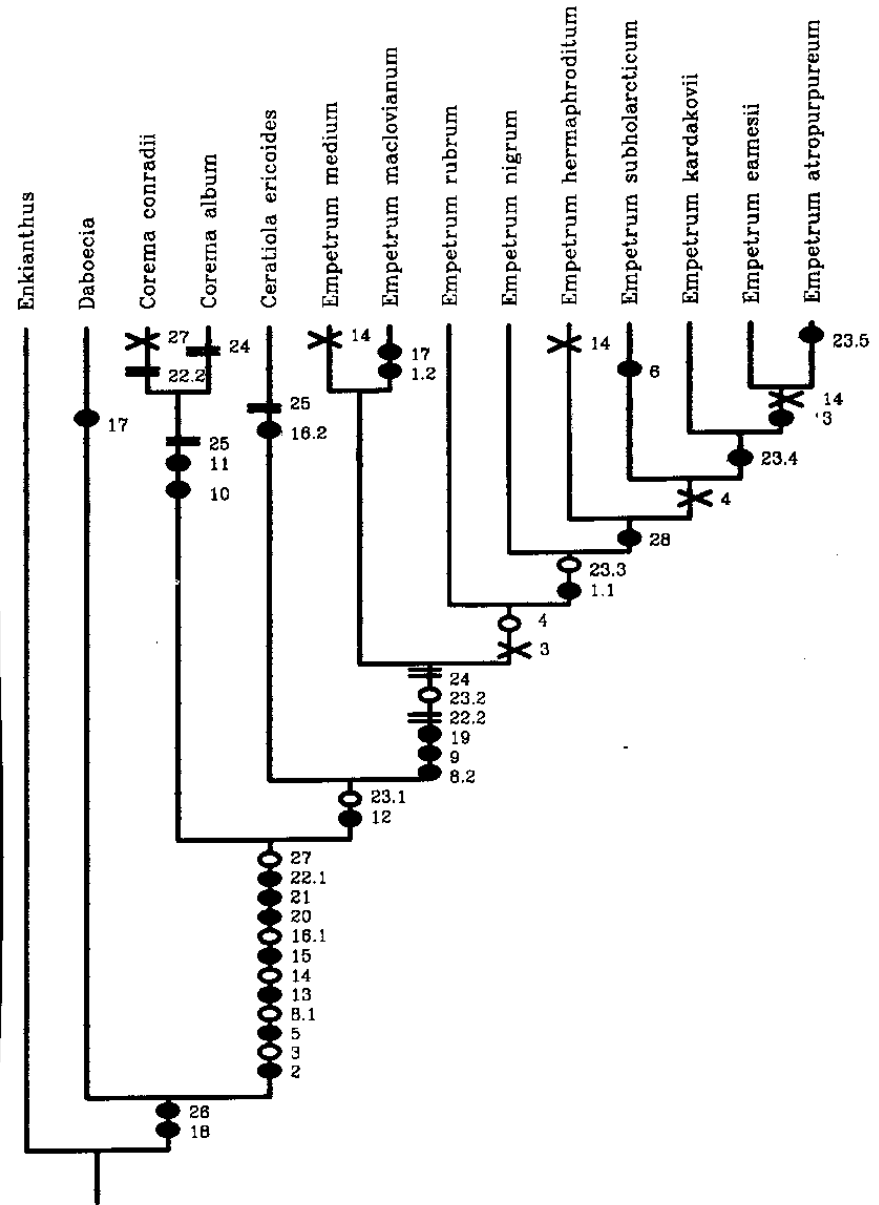
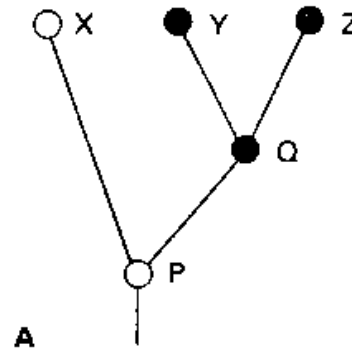
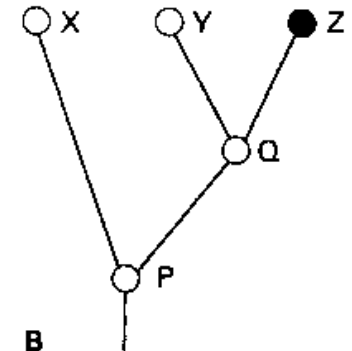


FIG. 2. One of five equally parsimonious cladograms of the Empetraceae. *Enkianthus* and *Daboecia* are outgroup taxa. Characters are numbered in accordance with the text, Appendix 1, and with Table 1. Black dots = synapomorphies ($ci = 1$), white dots = synapomorphies ($ci < 1$), parallel lines = parallelisms, crosses = reversals.

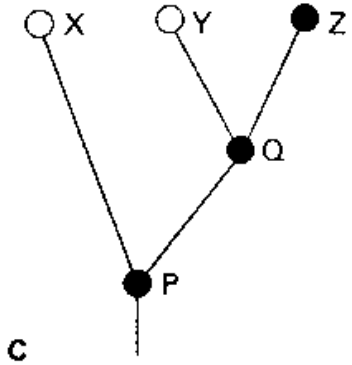
A Y-Z, X-Y-Z
monophyletic groups



B X-Y paraphyletic
groups



C X-Y polyphyletic
groups, paralelisms



D X-Y polyphyletic
groups, convergences

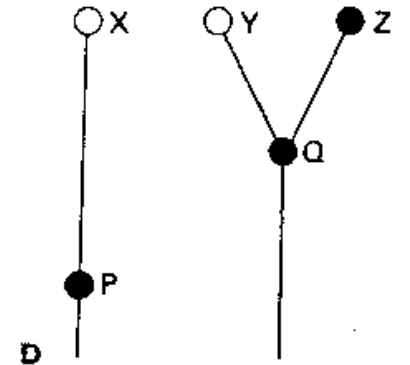


Fig. 2.6 Four diagrams showing different origins of three species (X, Y, Z) from the ancestral taxa P and Q in order to illustrate the concepts of monophyly, paraphyly, polyphyly, parallelism and convergence. The possession of one or other of two contrasting character-states by each of the five taxa is indicated by an open or closed circle respectively. **A.** Groups YZ and XYZ are both monophyletic; the similarity between Y and Z is a synapomorphy; the difference between X and YZ is due to divergence. **B.** Group XY is paraphyletic; group XYZ is monophyletic; the similarity between X and Y is a symplesiomorphy; the difference between Y and Z is due to divergence. **C.** Group XY is polyphyletic; group XYZ is monophyletic; the similarity between X and Y is a false synapomorphy caused by parallelism. **D.** Groups XY and XYZ are both polyphyletic; group YZ is monophyletic; the similarity between X and Y is a false synapomorphy caused by convergence.

- **Primitive character state**

Plesiomorphy

Symplesiomorphy

- **Derived character state**

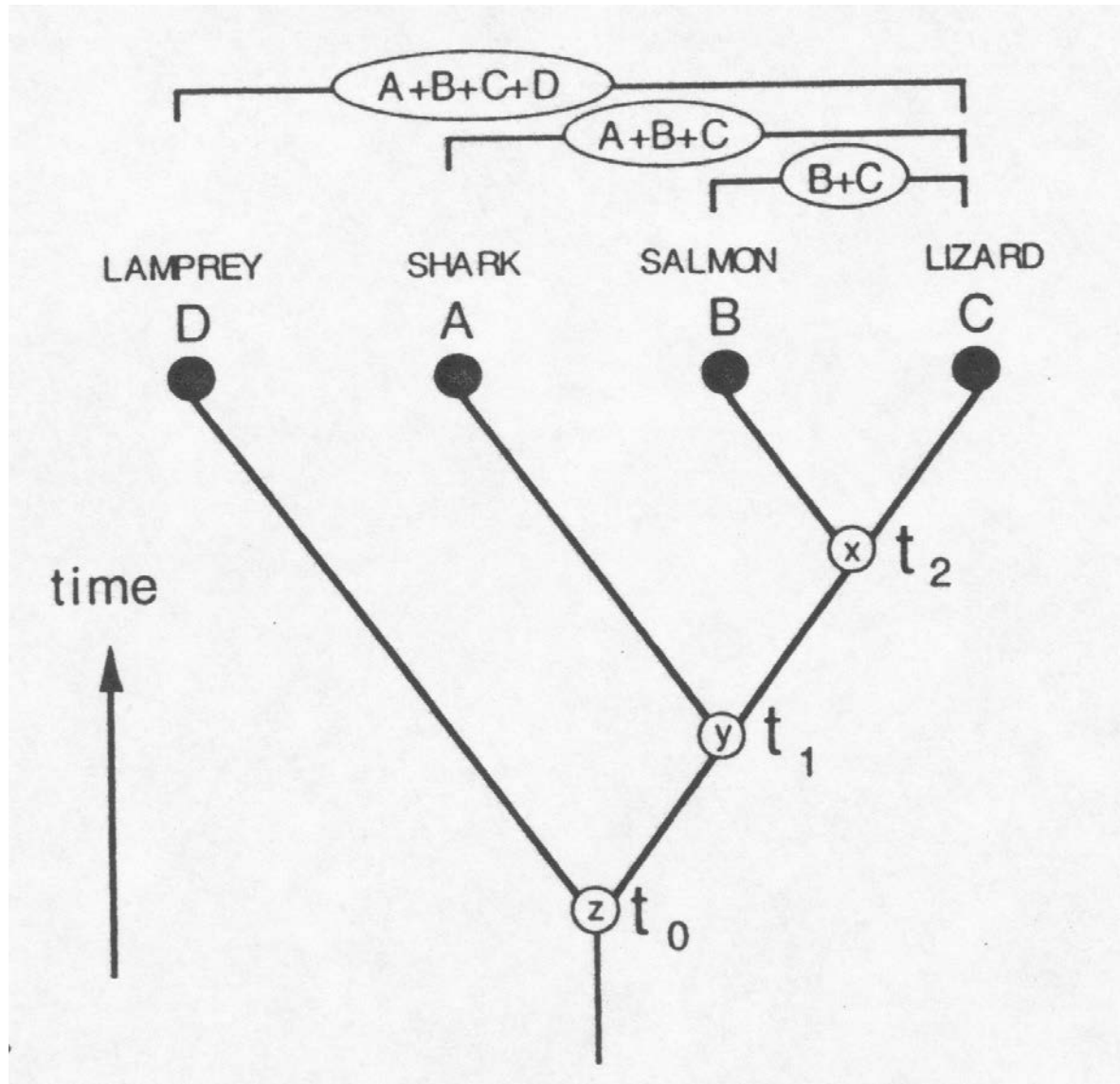
Apomorphy

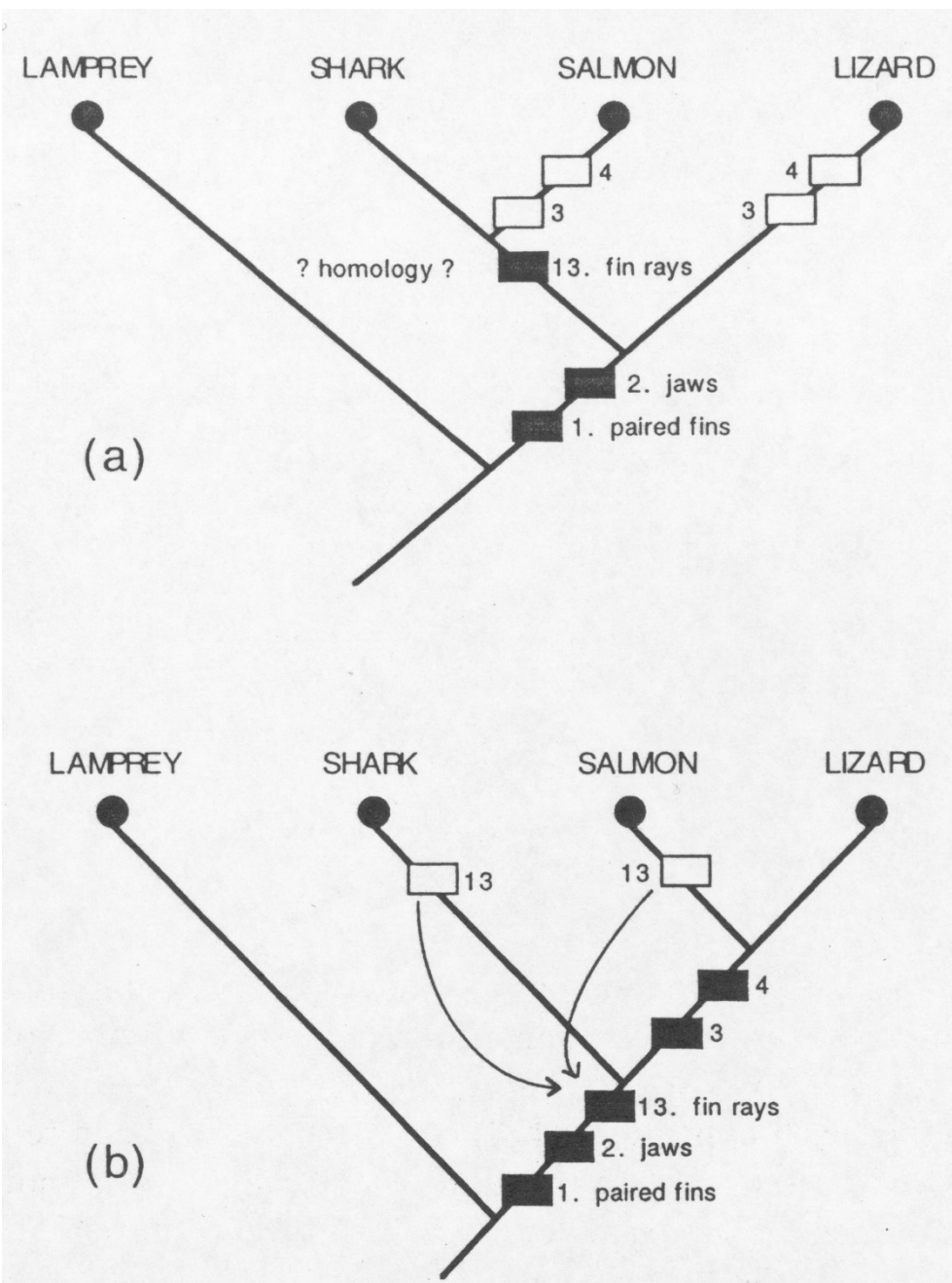
Autapomorphy

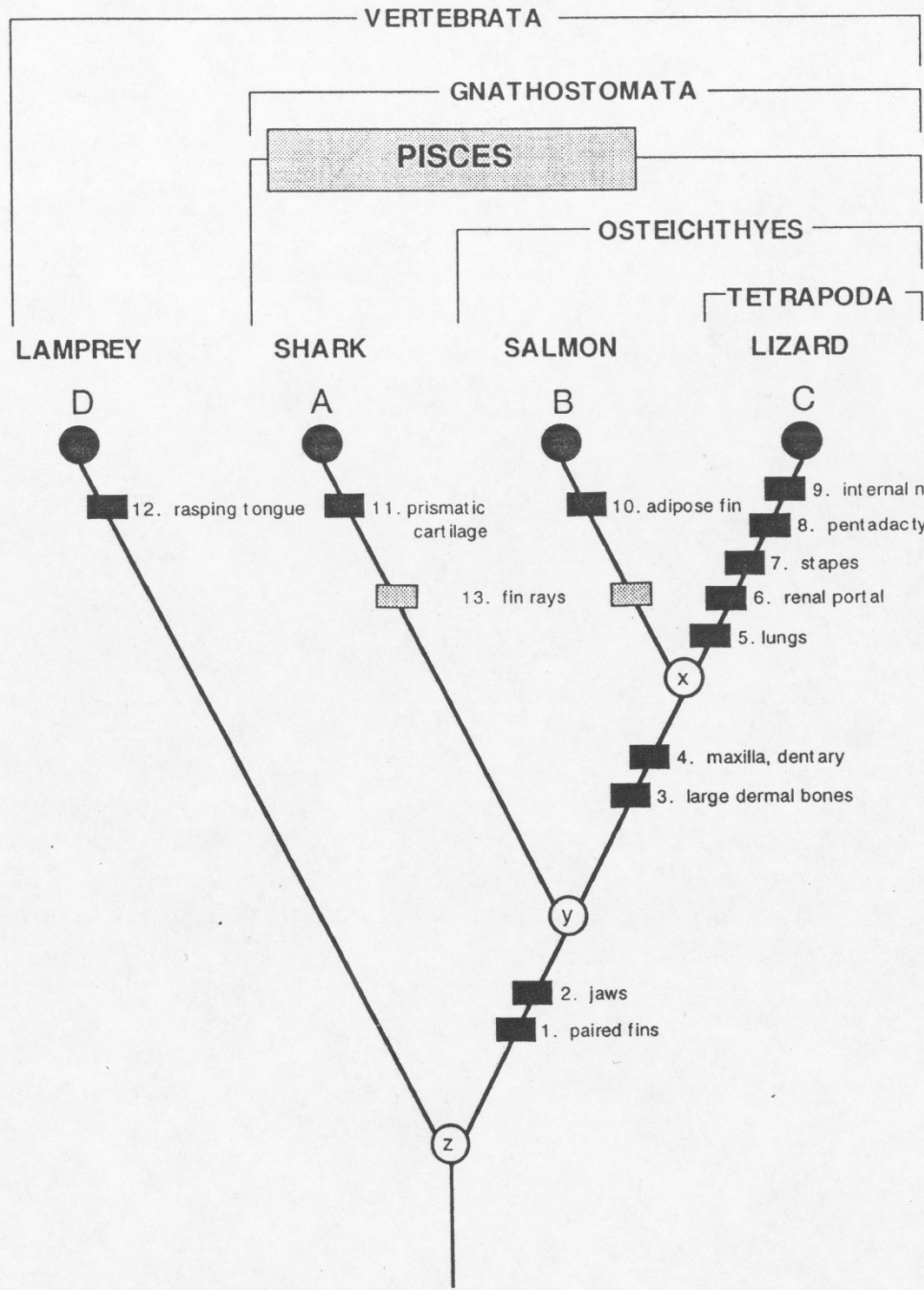
Synapomorphy

- **Homoplasy** = convergences + parallelisms

- **Outgroup comparison**







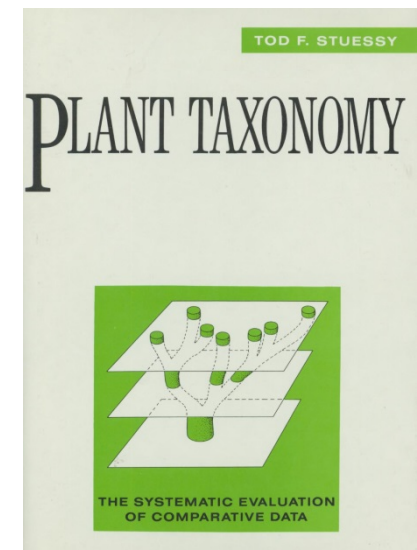
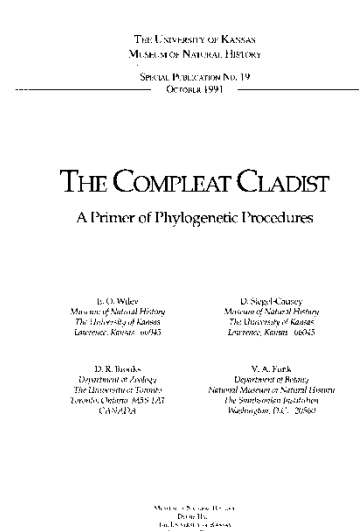
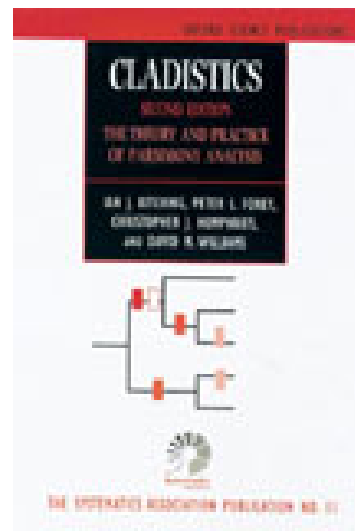
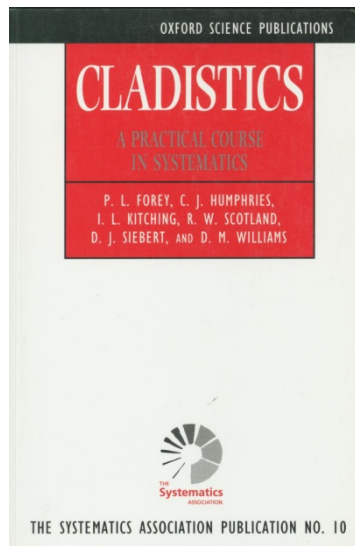
Forey, P.L., Humphries, C.J., Kitching, I.J., Scotland, R.W., Siebert, D.J. & Williams, D.M., 1992. *Cladistics. A practical course in systematics*. Clarendon Press, Oxford.

Kitching, I.J., Forey, P.L., Humphries, C.J. & Williams, D.M., 1998. *Cladistics. The theory and practice of parsimony analysis*. Ed. 2. Oxford University Press, Oxford.

Stuessy, T. F. 1990. *Plant taxonomy: the systematic evaluation of comparative data*. Columbia University Press, New York.

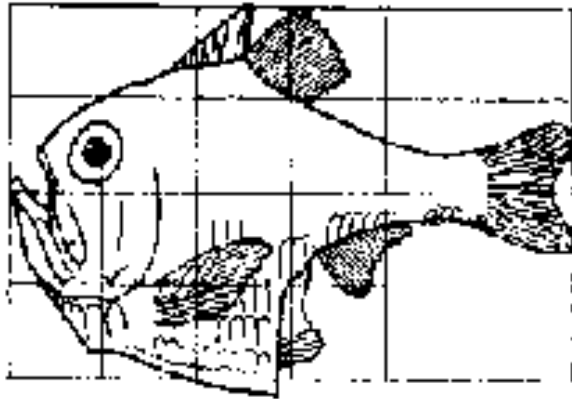
Wiley, E.O., Siegel-Causey, D., Brooks, D.R. & Funk, V.A. 1991. *The compleat cladist, a primer of phylogenetic procedures*. The University of Kansas, Museum of Natural History, Lawrence.

K dispozícii na www stránke: <http://nhm.ku.edu/cc.html>

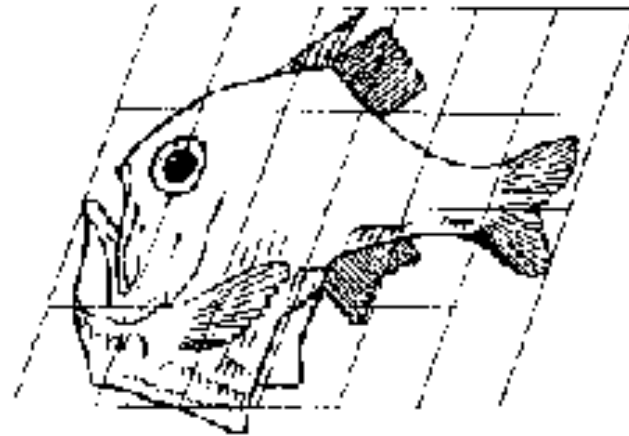


Geometric morphometrics

Thompson, A. W. 1917. *On growth and form.* Cambridge University Press, Cambridge.

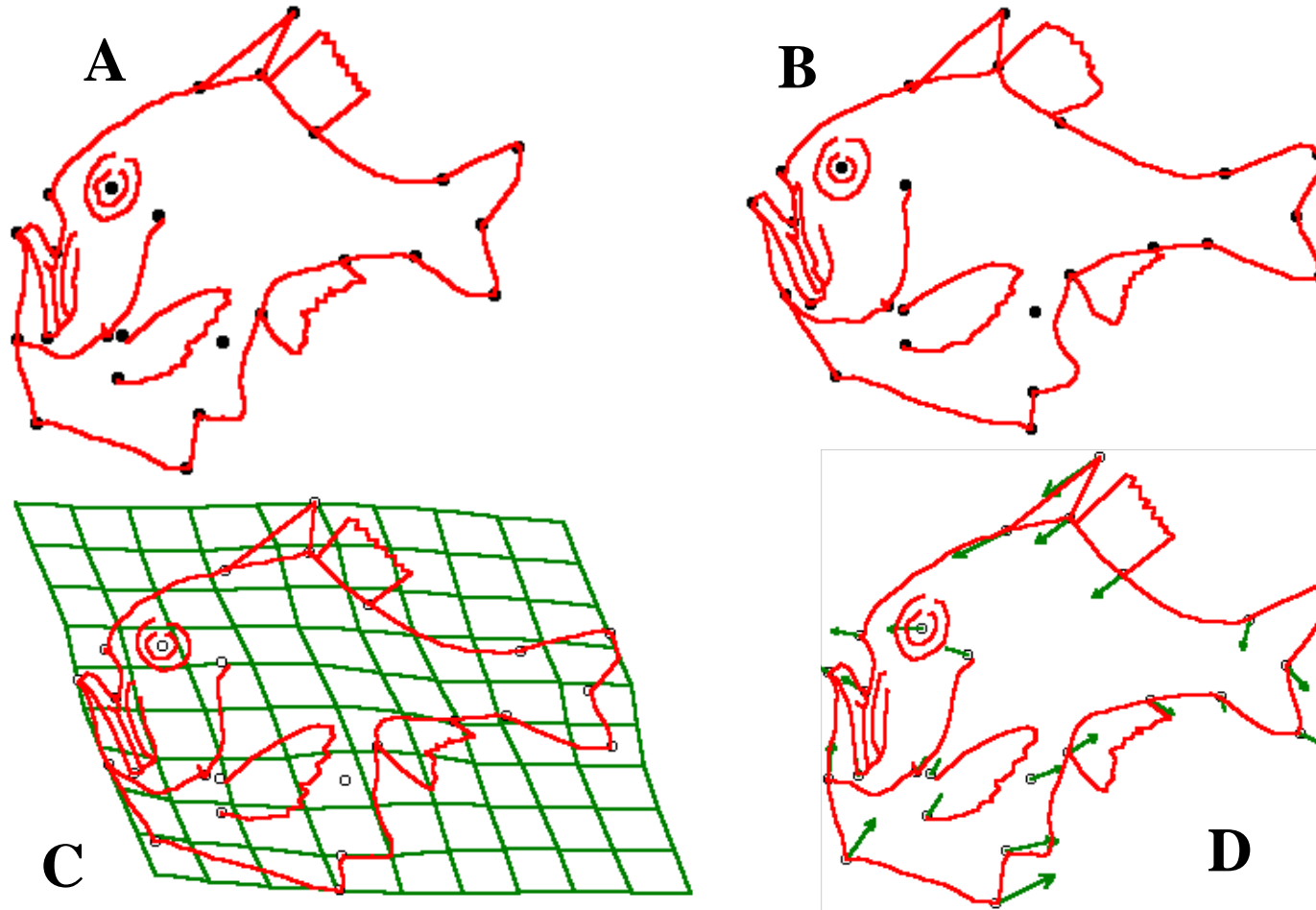


Argyropelecus olfersi.



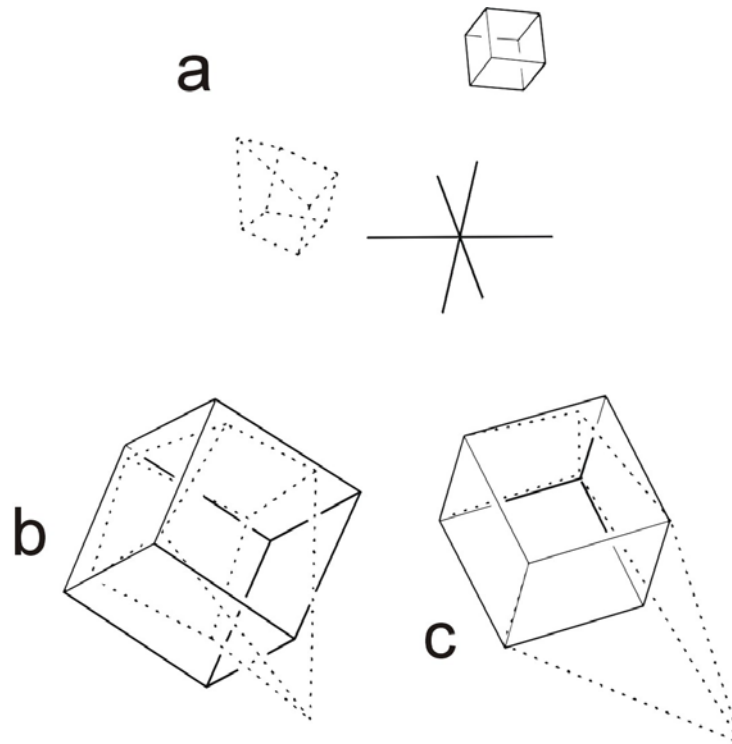
Sternoptyx diaphana.

Geometrická morfometrika



Mutual relationships of the shapes of the species *Stenoptyx diaphana* (A) and *Argyropelecus olfersi* (B) – sample data from the program tpsSpline (<http://life.bio.sunysb.edu/morph/>), C – visualization of the overall transformation using thin-plate spline, D – the same expressed using vectors.

Geometric morphometrics



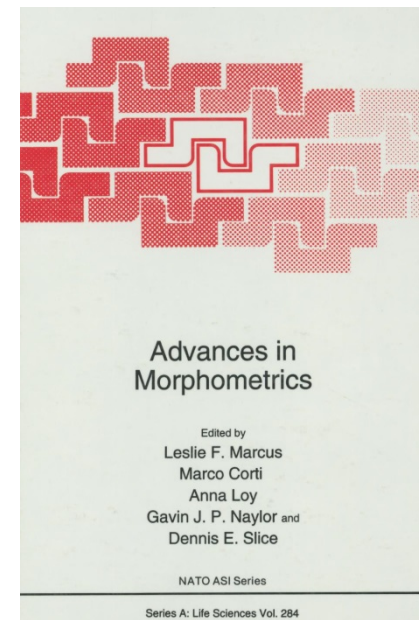
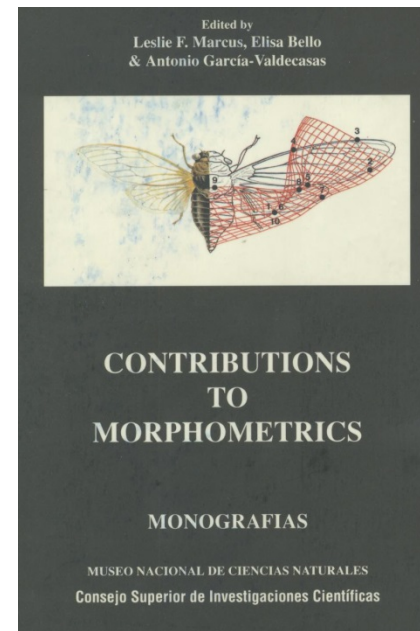
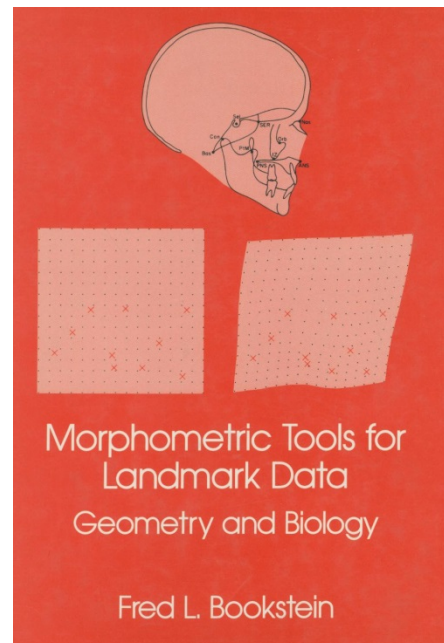
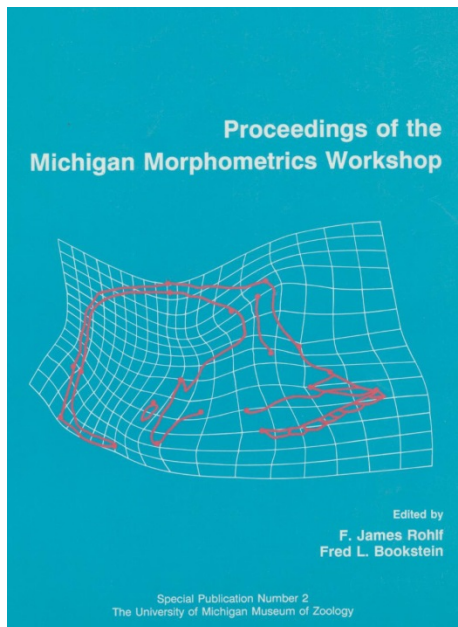
a – consensus configuration with a solid line, individual object dotted;
b – superposition using the GLS method (differences in the position of corresponding landmark points are comparable);
c – superposition using the resistant fitting method (objects differ significantly in the position of a single point).

Rohlf, F.J. & Bookstein, F.L., eds., 1990. Proceedings of the Michigan morphometric workshop. *Special Publ. No. 2, The University of Michigan Museum of Zoology*. [Blue book]

Bookstein, F.L. 1991. *Morphometric tools for landmark data: geometry and biology*. Cambridge University Press, New York. [Red book]

Marcus, L.F., Bello, E. & García-Valdecasas, A., eds., 1993. *Contributions to morphometrics*. Museo Nacional de Ciencias Naturales, Madrid. [Black book]

Marcus, L.F., Corti, M., Loy, A., Naylor, G.J.P. & Slice, D.E., eds., 1996. *Advances in morphometrics. NATO ASI Series A: Life Sciences 284*. [White book]



Macleod, N & Forey, P. 2002. *Morphology, shape and phylogeny*. Taylor and Francis, London, New York.

Macholán, M. 1999. Prokrustes, deformace a nová morfometrie. *Vesmír* 78: 35-39.